



The “Net Benefit” and the correlation between benefits and harms



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Problem

Benefit / risk assessments use *marginal* estimates that do not account for the correlation between the outcomes (benefits / risks)

Positive correlation

Example: skin rash in patients with EGFR-mutated advanced lung cancer receiving inhibitors of EGFR

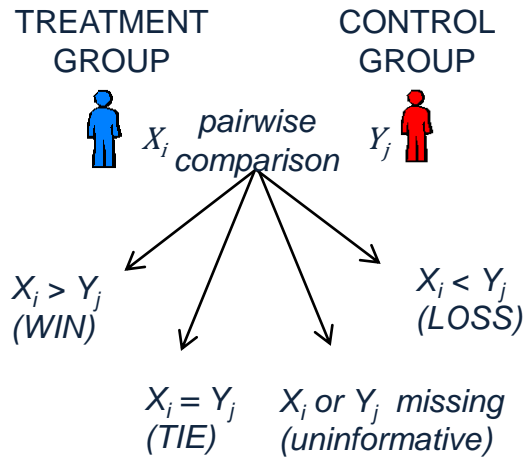
No correlation

Example: cardiac toxicity in frail patients with advanced breast receiving anthracyclines

Negative correlation

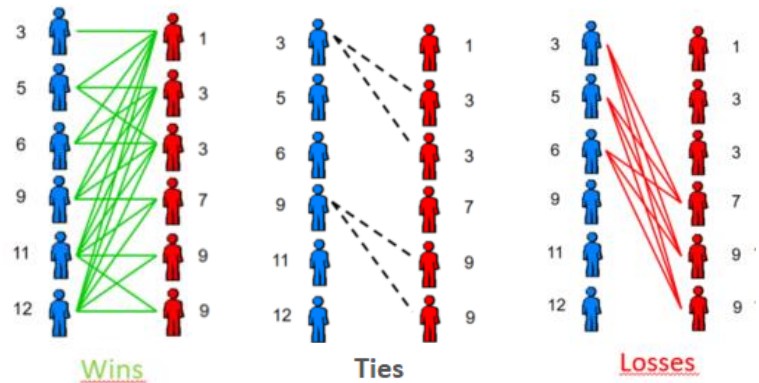
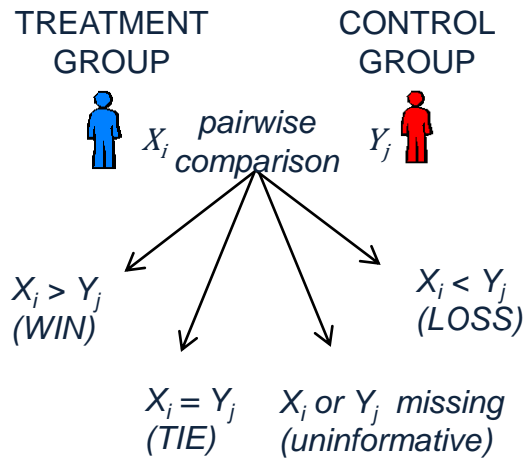
Example: toxicities leading to treatment stop in enzyme-deficient patients with advanced colorectal cancer receiving irinotecan

Pairwise Comparisons

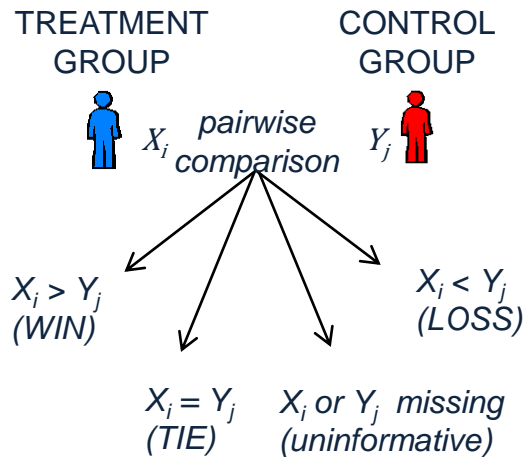


WINS $X_i > Y_j$
LOSSES $X_i < Y_j$
TIES $X_i = Y_j$
(UNINFORMATIVE)

All Pairwise Comparisons



Net Benefit



$$Net\ Benefit = \frac{\#Wins}{\#Pairs} - \frac{\#Losses}{\#Pairs}$$

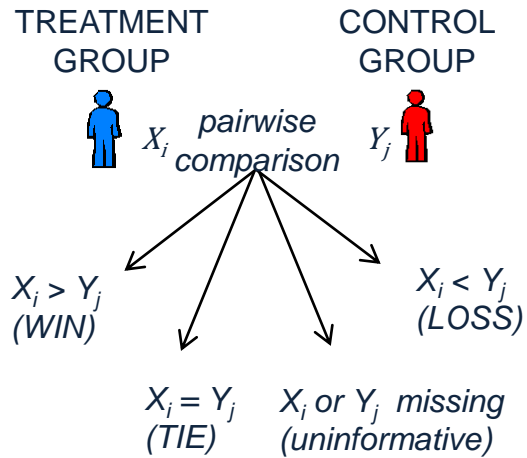
$$= 2\theta - 1$$

where θ is the « probabilistic index »

$$-1 < Net\ Benefit < 1$$

Net Benefit: probability that a random patient receiving Treatment does better than a random patient receiving Control, minus the probability of the opposite situation

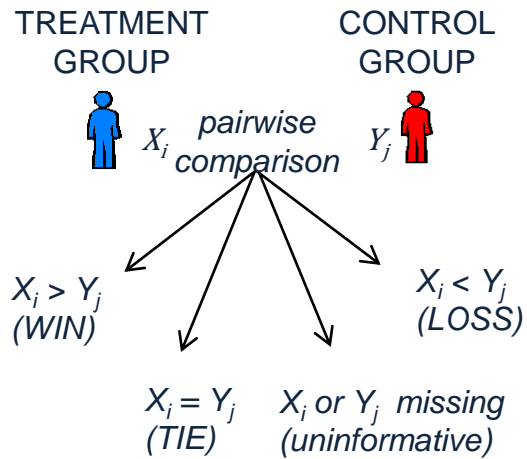
Win Ratio



$$\text{Win Ratio} = \frac{\#Wins}{\#Losses}$$

$$0 < \text{Win Ratio} < \infty$$

Win Odds



$$\begin{aligned} \text{Win Odds} &= \frac{\#Wins + \#Ties/2}{\#Losses + \#Ties/2} \\ &= \frac{\theta}{1-\theta} \end{aligned}$$

$$0 < \text{Win Odds} < \infty$$

The Net Benefit is a U-statistic

$$X_i \ (i = 1, \dots, m)$$

$$Y_j \ (j = 1, \dots, n)$$

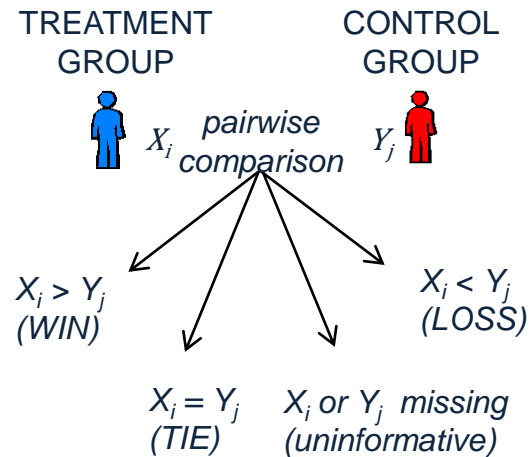
$$u_{ij} = \begin{cases} +1 & \text{if } (X_i, Y_j) \text{ pair is a win} \\ -1 & \text{if } (X_i, Y_j) \text{ pair is a loss} \\ 0 & \text{otherwise} \end{cases}$$

$$U = \frac{1}{mn} \sum_{i=1}^m \sum_{j=1}^n u_{ij}$$

U , the Net Benefit, is unbiased and efficient in situations of practical interest

GENERALIZATIONS

1 - Thresholds of Clinical Relevance



WINS

$$X_i - Y_j > \tau$$

LOSSES

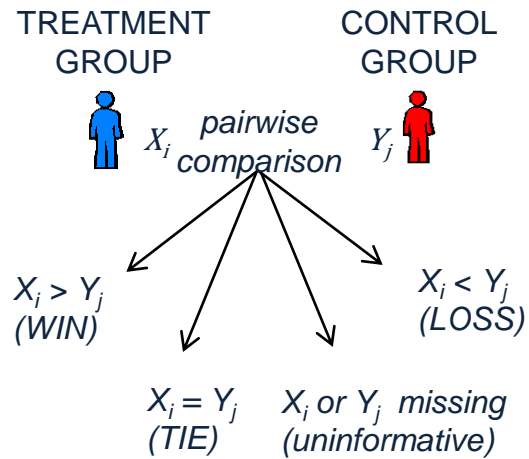
$$X_i - Y_j < -\tau$$

TIES

$$|X_i - Y_j| < \tau$$

GENERALIZATIONS

2 – Outcomes of Any Type



$>$ denotes « better outcome »

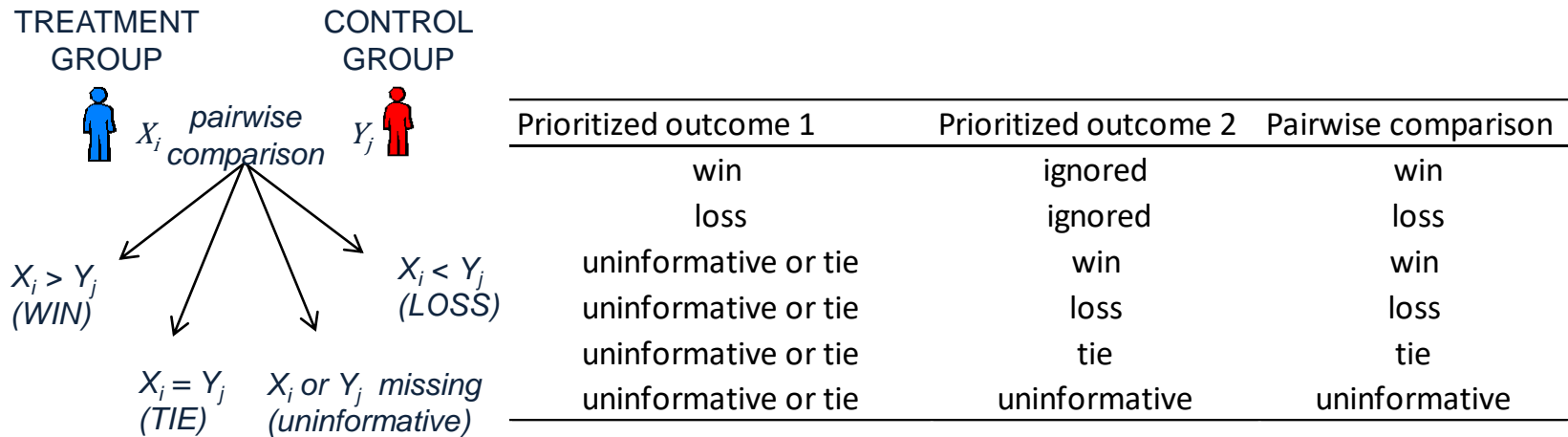
$<$ denotes « worse outcome »

WINS $X_i > Y_j$

LOSSES $X_i < Y_j$

GENERALIZATIONS

3 – Multiple Prioritized Outcomes

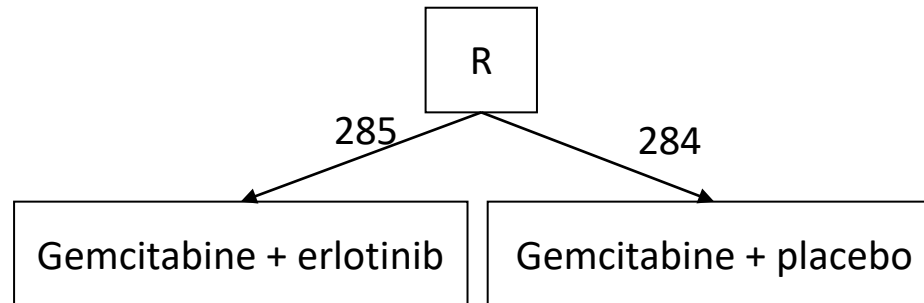


Ref: Finkelstein and Schoenfeld *Stat Med* 1999; Wittkowski et al. *Stat Med* 2004; Buyse *Stat Med* 2010

Benefit/Risk Analyses

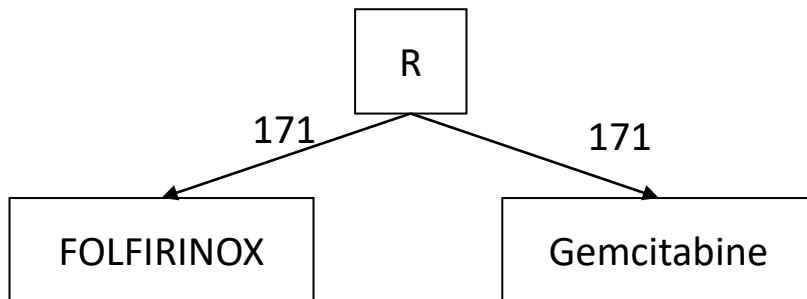
Erlotinib

569 advanced pancreatic cancers



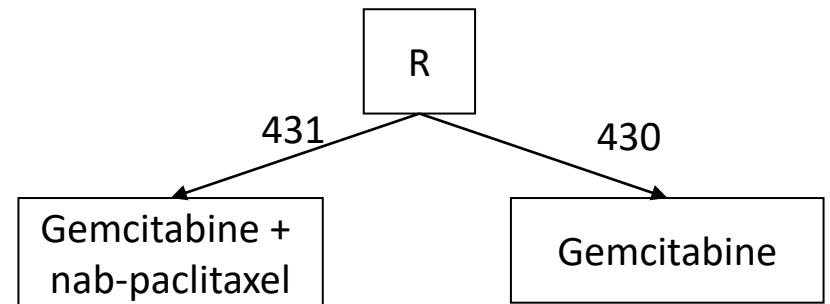
FOLFIRINOX

342 advanced pancreatic cancers

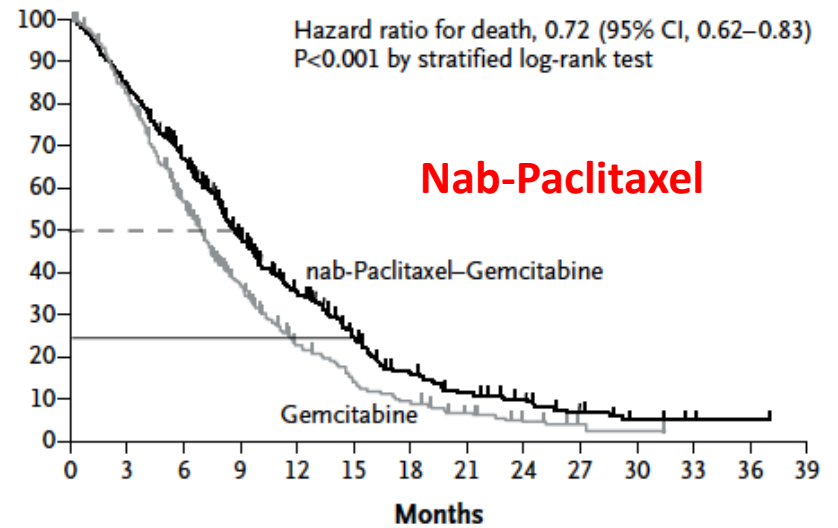
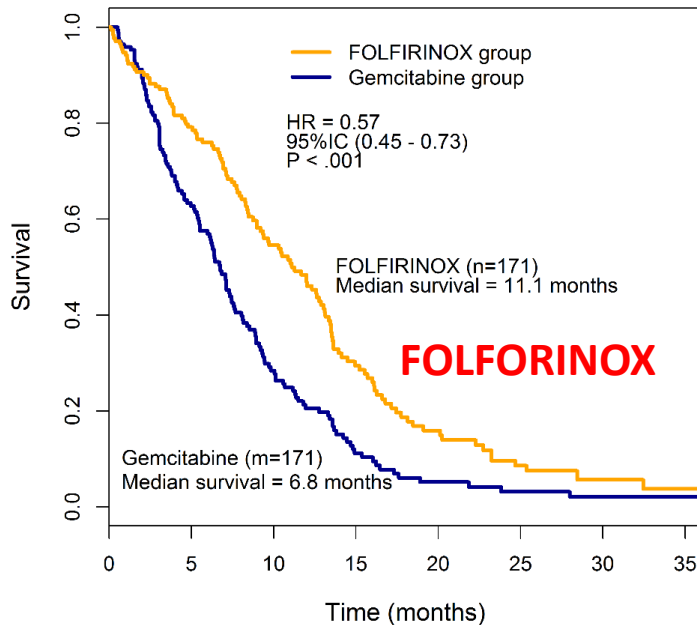
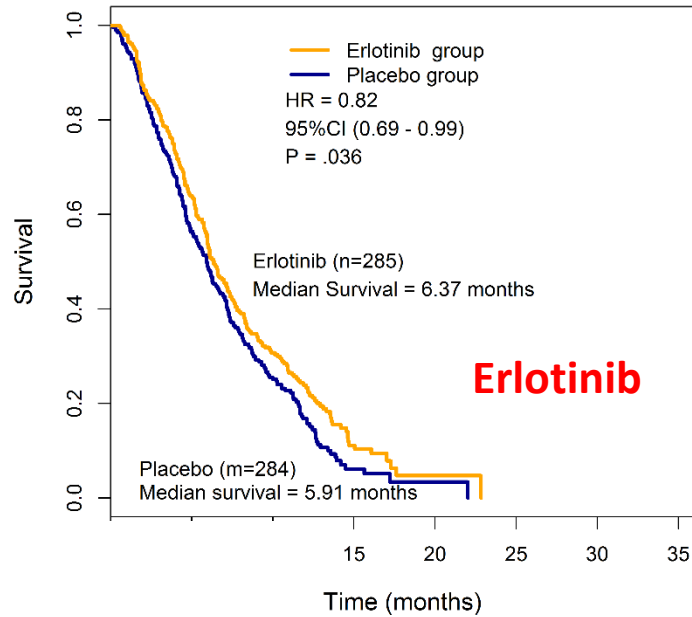


Nab-Paclitaxel

861 advanced pancreatic cancers



Benefit : Longer OS



Risk : Severe Toxicity

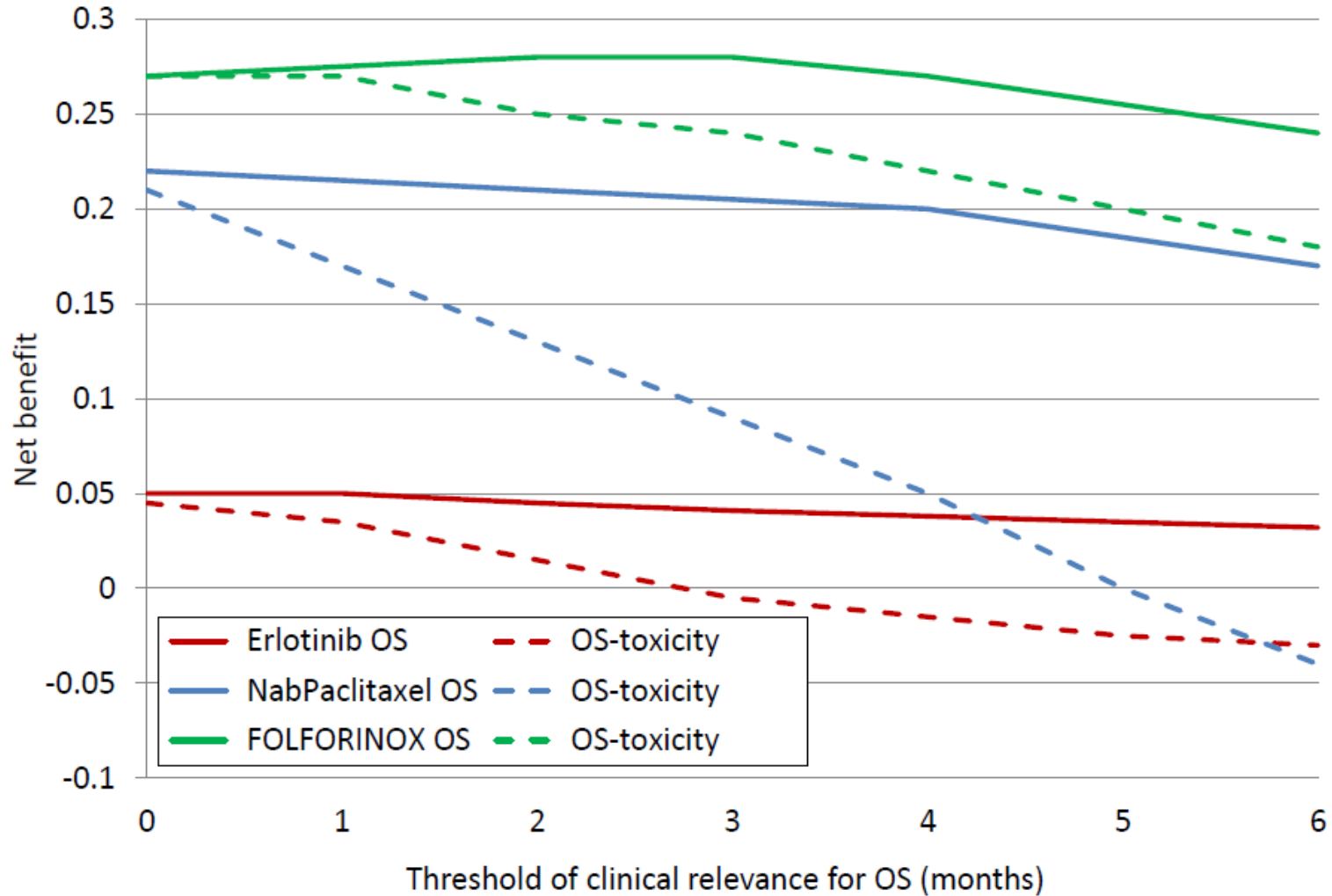
Erlotinib

FOLFORINOX

Nab-Paclitaxel

Worst Toxicity	Erlotinib	Gem	FOLFORINOX	Gem	Gem+NabP	Gem
None	10%	23%	4%	1%	9%	22%
Grade 1-2	59%	57%	27%	39%	36%	54%
Grade 3-5	31%	20%	69%	60%	55%	24%

Clinical Thresholds for OS



Conclusions

The Net Benefit, estimated with Generalized Pairwise Comparisons

- is flexible
- can incorporate multiple prioritized outcomes
- can incorporate thresholds of clinical relevance
- provides a mathematically correct benefit / risk assessment
- is meaningful to patients

Selected References

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