

# TIME-VARYING TREATMENTS IN OBSERVATIONAL STUDIES: LESSONS FOR CLINICAL TRIALS

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- Estimands
- Observational studies: **assumptions** and methods
  - Treatment rules
  - Endpoints
- Lessons for RCTs
- Conclusions

# Preliminaries

- I am a statistician working on theory and methods for the analysis of observational data in epidemiology
- I have no particular expertise in clinical trials
- ICH E9 Addendum:
  - Makes many good and important points
  - Some unfortunate choices of terminology ignoring much existing literature
  - Some important omissions

# Estimands?

- What is the aim of our analysis / what is our research question? Target of inference?
  - “Estimand” = what we want to estimate
    - Also (in statistical theory): what an estimator estimates when **assumptions** (not) satisfied
- ⇒ May or may not be a **parameter** parameterising (a part of) our model

# Estimands – in RCTs

- In RCTs, need to decide on estimand especially with view to “intercurrent events”:
    - alternative treatments / rescue medication
    - discontinuation of treatment
    - switching
    - dropout
    - terminal events / competing risks
- ⇒ occurrence after randomisation – **source of bias**

# Causal Estimand

= **“treatment rules”** to be compared

(individual interventions, combinations of interventions,  
regimen of sequence of interventions)

aka: “treatment strategies”

+ target population / subgroups

+ well defined **outcome(s) / endpoint(s)**

+ desired statistical contrast  
(e.g. survival probs. vs HR)

# Observational Studies

Early HIV studies (1990/2000s) (Swiss HIV Cohort Study!)

- No RCTs available, but treatment decisions required
- “Effect” of ART on time to AIDS / survival?
- Varying start of treatment (CD4 / viral load)
- Issues
  - Severe side-effects, non-adherence
  - Per protocol: “always” versus “never” treat?
  - When best to start?
  - When best to switch? (in view of failure / resistance)
- Main motivation for **marginal structural models**

Hernan et al (2000); Cain et al (2016); Gran et al (2010)

# Observational Studies

Pharmaco-epidemiology (from health records / claims data)

- Post-accreditation safety / comparative effectiveness
- Wanted: long-term (side-)effect in general population (incl. vulnerable subgroups)
- Issues
  - Confounding by indication
  - Alignment of eligibility, treatment start, start of follow-up ambiguous
  - Combination of several medications, switching very common
  - Immortal time / prevalent user bias & other “self inflicted” biases
- Key example for **target trial emulation**

Hernan & Robins (2016), Labreque & Swanson (2017)



## Key characteristic:

- Exposure (treatment) is rarely a binary point-treatment; instead it is time-dependent (dynamic)
  - treatment / exposure often has a duration
  - can start / stop / start again / switch / combine etc.
  - often: want **adaptive** treatments
- Experience:  
trying to “force” this into simple binary point-treatment framework usually results in bias or practically irrelevant results

- Need to be clear what treatment rules (sequence of interventions) we want to contrast
  - Relevant duration “less than...” vs. “more than...”
  - “Always treat” versus “never treat”
  - “If... then...” rules
  - “Start treatment immediately” vs. “delay treatment until...”
- To obtain inference on the effect of such treatment rules from observational data, need
  - **defendable** assumptions
  - suitable methods

# How Do We Know What We Want?

Two (complementary) approaches:

Patient, doctor  
Public health authority  
(Regulatory agency?)

1. What is the **decision problem** you want to solve?

*(Dawid & Didelez, 2010; Dawid, 2015)*

- aim: compare the options between which to decide

2. What is the ideal experiment, **“target trial”**?

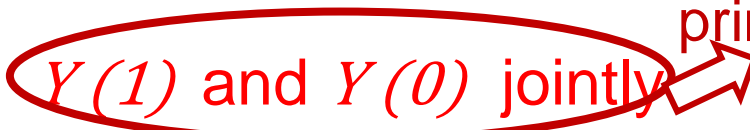
*(Hernan & Robins, 2016; Cain et al, 2016)*

- disregarding practical, ethical, financial, legal etc. constraints
  - but *in this world & respecting physical laws*
- ⇒ then emulate trial as closely as possible with available data

# How Do We Formalise What We Want?

Notation: to distinguish **intervention** from **observation**

Mathematically (here for **point** treatment  $X$ , endpoint  $Y$ ):


- potential outcomes  $Y(x)$ 
  - the **value** of  $Y$  if  $X$  were set to  $x$  by the intervention”
- **do-notation**  $P(Y; do(X=x))$  & **causal DAGs** (Pearl, 2009)
  - “the **distribution** of  $Y$  if  $X$  were set to  $x$  by the intervention”
- RCTs with randomised  $X$  & full compliance: directly observe  $P(Y(1))$  (treatment arm) and  $P(Y(0))$  (controls)
- Note: we **never** observe  $Y(1)$  and  $Y(0)$  jointly  **princ.stratum**  
be aware (and beware) of assumptions on joint distribution - *fundamentally untestable*. (Dawid, 2000)

# Formalising Treatment Rules

Consider treatments over two seq. time points:  $X_1, X_2$

## Treatment rule

= rule for assigning values  $x_1, x_2$  by seq. interventions

- Fixed in advance: “always  $(x_1=1, x_2=1)$  / never treat  $(x_1=0, x_2=0)$ ” or “stop early”  $(x_1=1, x_2=0)$
- Or **dynamic / adaptive / ...** :  
after  $X_1$ , observe  $Z=z$ , then assign  $x_2=g(z)$   “g-methods”
  - $Z$  could be CD4 count, side effect....

# Formalising Treatment Rules

- Estimand: contrasts of different treatment rules
  - taking intercurrent events into account
- **Example:** compare
  1.  $x_1$  = new drug,  $Z$  = occurrence of adverse event,  $x_2$  = switch to std. drug if  $Z=1$  else,  $x_2$  = new drug  
with
  2.  $x_1$  = std. drug,  $x_2$  = std. drug

# Identifiability Assumptions

Not mentioned in ICH E9 Addendum:

Under what **structural** assumptions can we identify our chosen estimand from observable data?

- in principle,  $N=\infty$
- non-parametrically
- In RCT: only treatment *assignment* is randomised
  - identifies ITT-based effects

Other assumptions (required by most approaches):

- **Consistency** → treatment rule “well-defined”
- **Positivity** → target treatment rules possible for all individuals
- **No unmeasured time-varying confounding**
  - aka “sequential randomisation”

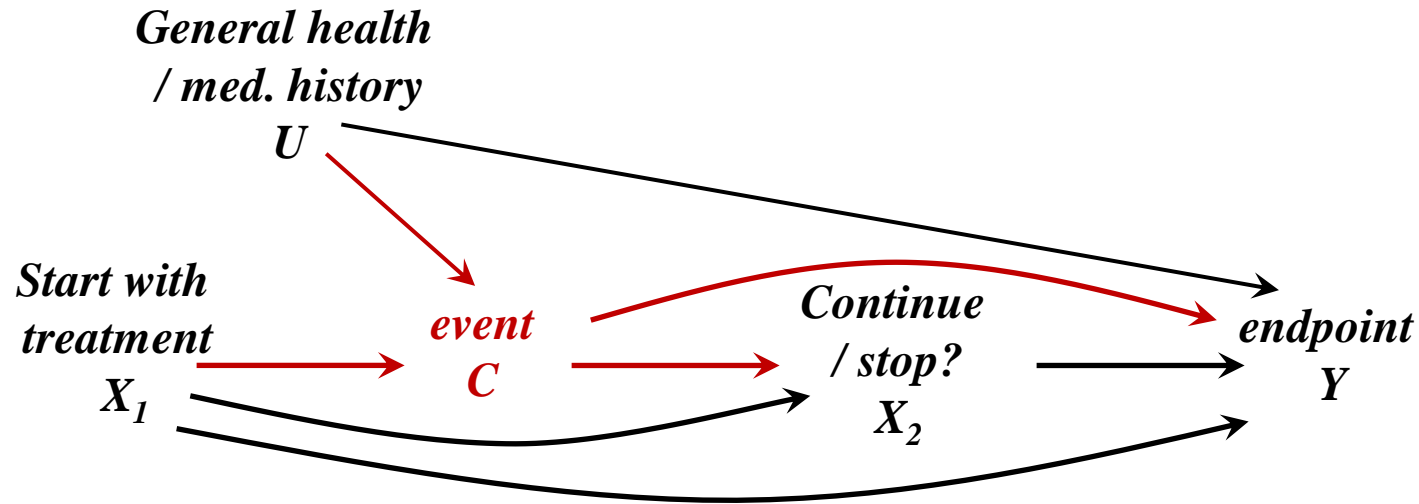
# Positivity Assumption

- Violated if chosen treatment rules cannot possibly occur for certain patients, e.g. “continue with treatment even under allergic reaction”
  - if allergic reaction is predictive of endpoint
- If violated, practical relevance of estimand debatable
  - alluded to in ICH E9 Addendum
- Mathematically:
  - we would extrapolate into area where we have no data
    - may not notice under parametric models
  - with “inverse-probability-weighting”: would divide by zero



# Time-Dependent Confounding

(Robins, 1986+)



- $C$  affected by prior treatment, confounding future treatment and endpoint
- Note:
  - $U$  can remain unmeasured if  $C$  is measured = “sequential randomisation” (cond. on  $C$ )
  - $U$  and  $X_1$  independent by randomisation

# Adjusting for Time-Dep. Confounding

- Cannot use:
  - Regression adjustment
  - (Propensity score) matching / stratification

Instead:

- g-formula
- MSMs fitted by IPW
  - time-varying weights

basic principles

⇒ Basis for many more advanced techniques

- Double robust estimation / g-estimation
- Targeted maximum likelihood
- ... combine with machine learning approaches

# g-Formula

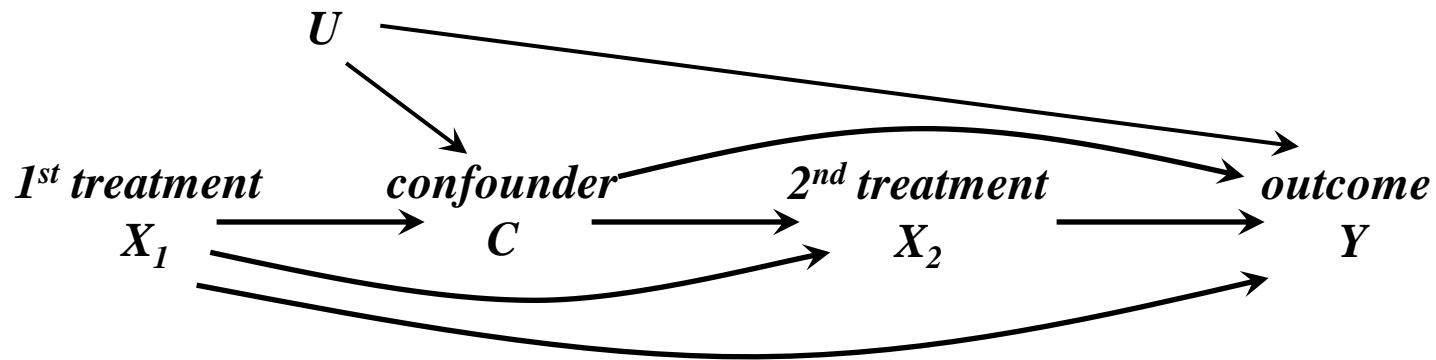
(Robins, 1986; reformulated: Dawid & Didelez, 2010)

- Need models for
  - $E(Y | X_1 = x_1, C=c, X_2 = x_2)$
  - $P(C | X_1 = x_1)$

For  $(X_1 = x_1, X_2 = x_2)$  as determined by treatment rule:

$$\sum_c E(Y | X_1 = x_1, C=c, X_2 = x_2) P(C | X_1 = x_1)$$

(early application: Robins, Hernan, Siebert, 2004)



# Inverse Probability of Treatment Weighting

- Assume marginal **structural** model (MSM)
  - for  $E(Y; \textit{treatment rule A})$  vs.  $E(Y; \textit{treatment rule B})$
  - or for dynamic strategy  $E(Y; g(\cdot))$
- Fit by weighting each obs. with **inverse** of prob. for observed treatment sequence

$$P(X_1 = x_1) P(X_2 = x_2 | C=c)$$

- re-weighted population: like randomised
- Special cases
  - Survival outcome – time-varying weights;
  - “Optimal” strategy – regret regression models, optimal MSMs


Murphy (2003), Chakraborty & Moodie (2013)

# “Quality of Life after Death”

- Intercurrent event: terminal (comp. risk)
- **Example:** want effect of treatment on cognitive function in the elderly
  - endpoint not observable if **death occurs first**
- Patient: might want to know whether treatment affects survival...
  - arguably, more important than cognitive function
- ICH E9: consider “composite”, i.e. combined endpoints
  - lessons from observational studies...?

# “Quality of Life after Death”

Sensible estimand?

- Not: subgroup = “alive” (selection bias)  
 - **except if death known to be unaffected by treatment!**
- Practically relevant: combine death & cognitive function
  - Utility function?
  - Note: joint distribution after randomisation is identified
- *Principal stratum* subgroup  **relevant subgroup?** “rs”  
 arguably not directly useful for decision making nor  
 implementable in target trial (Dawid & Didelez, 2011)

- New approach:  
**separable effects** (Didelez, 2019, Stensrud et al, 2020)

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# Conclusions

- There is no such thing as “a / the treatment effect”
- There are only contrasts of specified *treatment rules*
  - Most treatments in practice get changes / adapted over time
  - We should target treatment rules with practical relevance
  - Taking possible changes over time into account



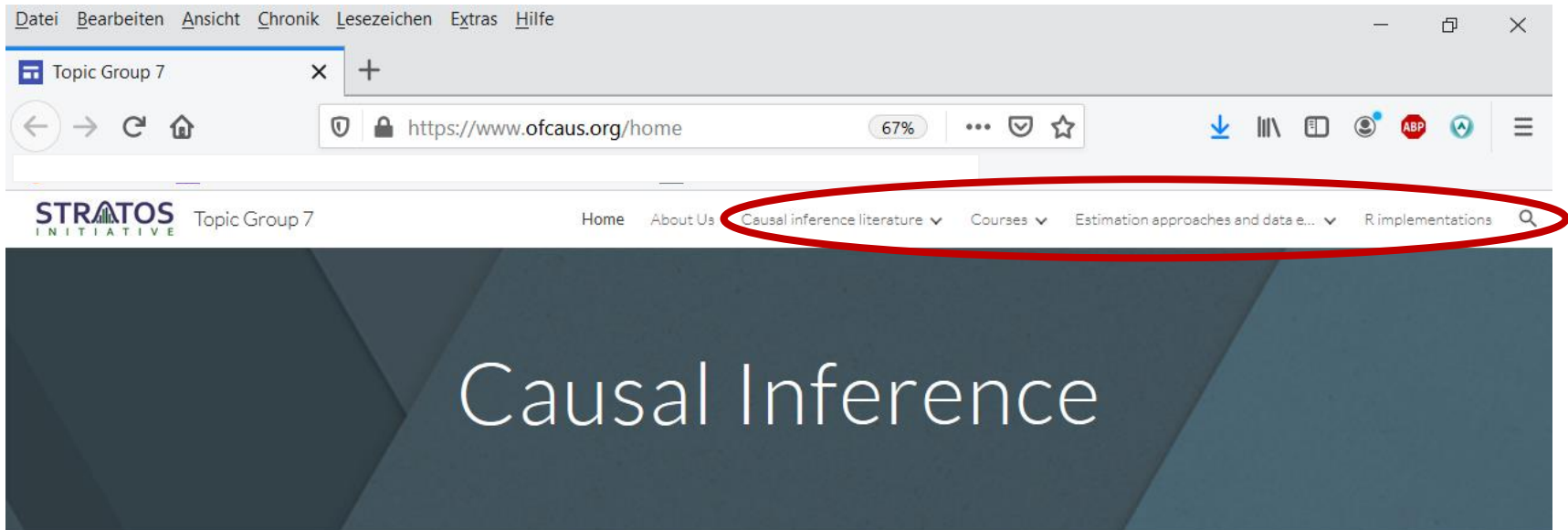
## *Design trumps analysis*

- When you *can* actually carry out your target trial, then do it!
  - Randomise between (dynamic / adaptive) treatment rules relevant for real practice, including possibilities of dealing with intercurrent events
  - ... this will also increase adherence [Scharfstein \(2019\)](#)
  - e.g. “treat with A except if Z happens, then switch to B” etc. if this best reflects real life decisions

# Implications for RCTs

- Statistical methods to compensate for (time-varying) confounding, or other “statistical tricks”, should only be used as last resort
- Collect enough information on reasons for intercurrent events
  - to plausibly assume “no unmeasured time-varying confounding”
  - especially: to characterise adherence

# Advert 1 – ofcaus.org



The screenshot shows a web browser window with the URL <https://www.ofcaus.org/home>. The browser's address bar and navigation icons are visible. The website header includes the STRATOS INITIATIVE logo on the left and a navigation menu on the right. The navigation menu items are: Home, About Us, Causal inference literature (highlighted with a red oval), Courses, Estimation approaches and data e..., and R implementations. Below the header is a large dark blue banner with the text "Causal Inference" in white.

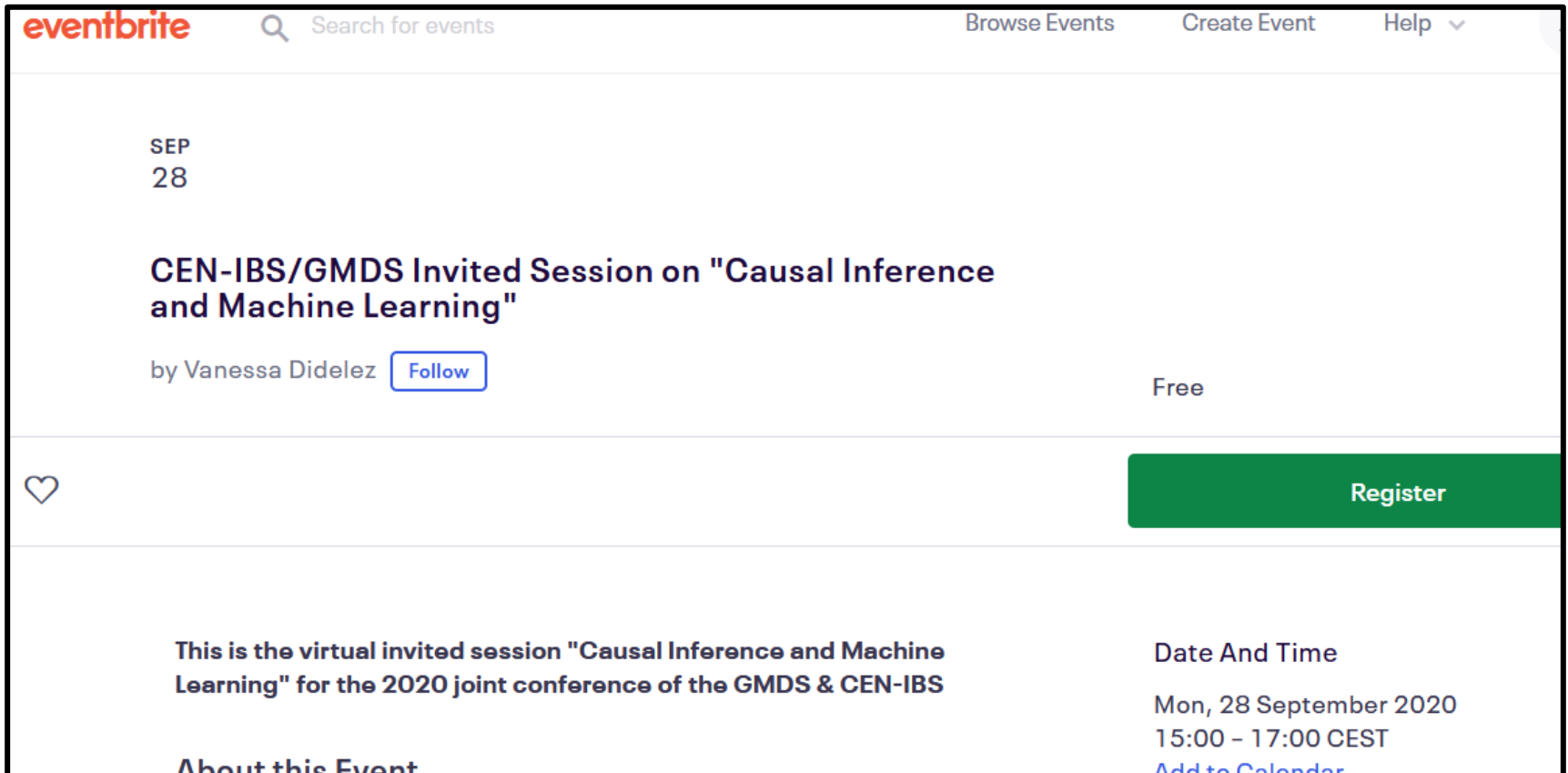


## STRATOS Initiative

Topic group 7 is a member of the [STRATOS Initiative](#) (STREngthening Analytical Thinking for Observational Studies) which is a large collaboration of experts in many different areas of biostatistical research. Ongoing research, discussions and activities within STRATOS are conducted in nine [topic groups](#) and several cross-cutting [panels](#).

# Advert 2 – Invited Session

- <https://www.eventbrite.de/e/cen-ibsgmds-invited-session-on-causal-inference-and-machine-learning-tickets-116222778459>



The screenshot shows the Eventbrite interface for an event. At the top, there is a navigation bar with the Eventbrite logo, a search bar, and links for 'Browse Events', 'Create Event', and 'Help'. Below the navigation bar, the event date 'SEP 28' is displayed. The event title is 'CEN-IBS/GMDS Invited Session on "Causal Inference and Machine Learning"', followed by the organizer 'by Vanessa Didelez' and a 'Follow' button. The price is listed as 'Free'. A green 'Register' button is prominently displayed. Below the main event information, there is a section titled 'This is the virtual invited session "Causal Inference and Machine Learning" for the 2020 joint conference of the GMDS & CEN-IBS'. To the right, the 'Date And Time' is specified as 'Mon, 28 September 2020 15:00 - 17:00 CEST'. At the bottom, there are links for 'About this Event' and 'Add to Calendar'.

# Thanks!

[www.leibniz-bips.de/en](http://www.leibniz-bips.de/en)

## Contact

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- *and find many more discussions in that journal*