



# Component network meta-analysis compared to a matching method in a disconnected network: a case study

Gerta Rücker<sup>1</sup>, Susanne Schmitz<sup>2</sup>, Guido Schwarzer<sup>1</sup>

<sup>1</sup> Institute of Medical Biometry and Statistics, Faculty of Medicine and Medical Center – University of Freiburg, Germany

e-mail: [ruecker@imbi.uni-freiburg.de](mailto:ruecker@imbi.uni-freiburg.de)

<sup>2</sup> Competence Center for Methodology and Statistics, Department of Population Health, Luxembourg Institute of Health, Strassen, Luxembourg

DFG research project RU1747/1-2

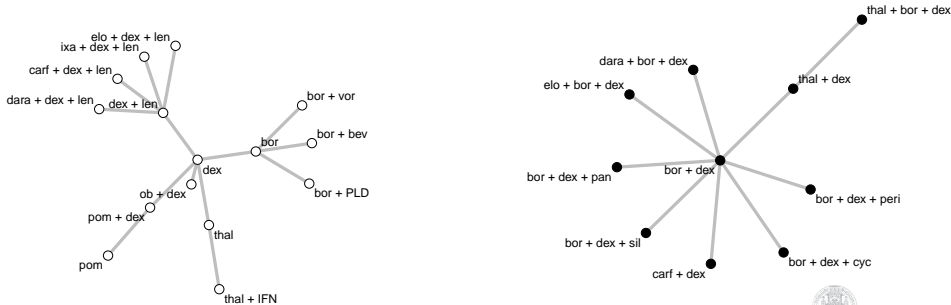
Basel, 04. February 2020

# Outline

- 1 Background: A disconnected network**
- 2 Separate network meta-analyses**
- 3 Matching method**
- 4 Component network meta-analysis**
- 5 Results**
- 6 Discussion**
- 7 Summary**

# A disconnected network

- Network meta-analysis (NMA) of 25 trials investigating treatments and treatment combinations for multiple myeloma [Schmitz et al., 2018]
- Outcome: Progression-free survival, relative effects measured as hazard ratios (HR)
- Encountered two separate networks, the "white network" (left, 15 treatments) and the "black network" (right, 10 treatments)



# A disconnected network

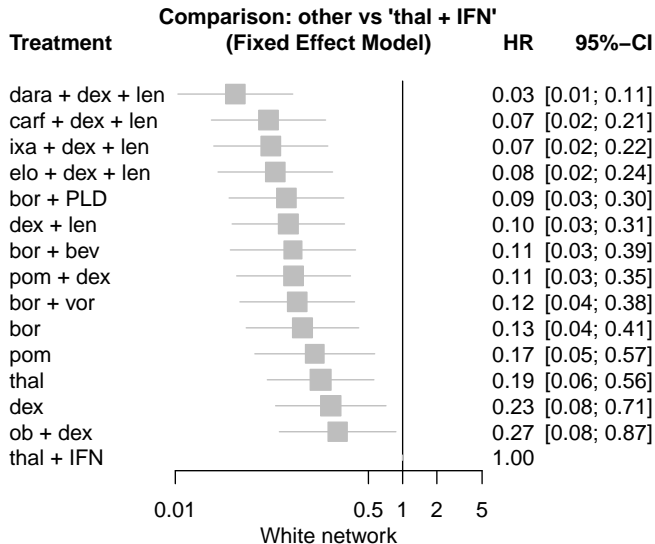
The "white network" and the "black network" have no treatments in common

How to deal with that in a network meta-analysis?

- Separate NMA analyses
- Matching method [Schmitz et al., 2018]
- Component network meta-analysis [Welton et al., 2009, Rucker et al., 2019b]

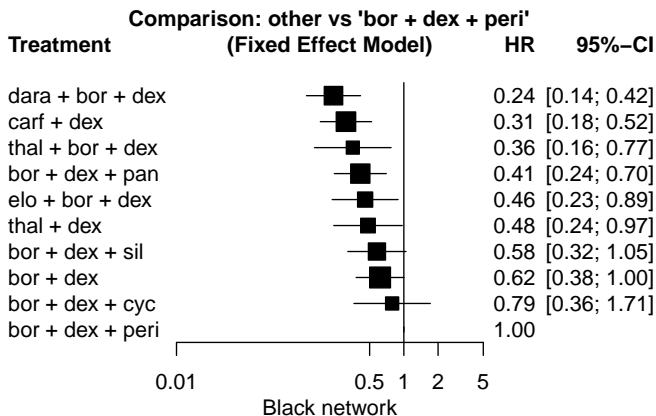
# Separate network meta-analyses

”White network”



# Separate network meta-analyses

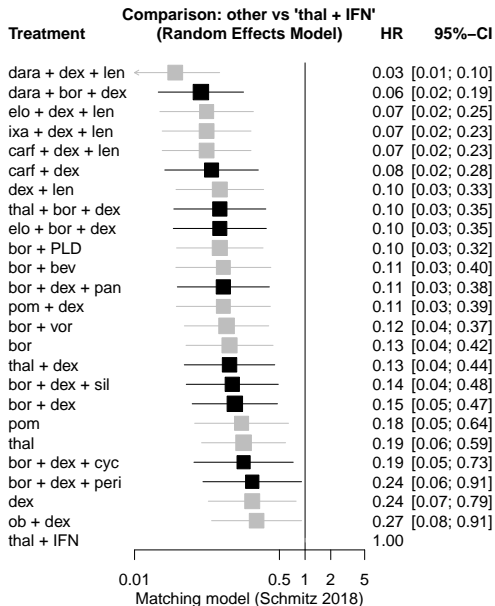
”Black network”



## Matching method [Schmitz et al., 2018]

- Sought evidence from observational studies to connect the disconnected network
- In the absence of comparative observational studies, single-arm studies were considered
- Distance metric based on covariate profiles allowed measuring similarity between studies (treatment history, age, baseline stage, gender)
- Five matches between the networks could be identified
- Models fitted in WinBUGS using the R package R2WinBUGS [R Core Team, 2019, Sturtz et al., 2005]

# Matching method





# Component network meta-analysis

- Standard model of network meta-analysis:  
Each treatment is represented by one node in the network
- However, treatments may be complex, for example, combinations of other treatments (multicomponent interventions)
- This was observed in the Multiple Myeloma case study
  - White network: dara + dex + len, carf + dex + len, bor + bev, thal + IFN, ...
  - Black network: dara + bor + dex, carf + dex, bor + dex, thal + dex, ...
- ⇒ **Component network meta-analysis (CNMA)**  
[Welton et al., 2009, Rucker et al., 2019b]

# Additive CNMA Model [Rücker et al., 2019b]

- Consider two **active components**:
  - **pom** pomalidomide
  - **dex** dexamethasone
- Three possible **treatment combinations**:
  - 1 **pom**
  - 2 **dex**
  - 3 **pom + dex**
- **Additive model**: The effect of the combined treatment is an additive sum of its components
  - This means that 'equal components cancel out':  
**pom + dex** vs. **dex** estimates **pom**
  - Example for three components:  
**carf + dex + len** vs. **dex + len** estimates **carf**

# Additive CNMA model

Introductory example:

- $n = 3$  **treatments**, interpreted as additive combinations from
- $c = 2$  **components**
- $m = 4$  **pairwise comparisons** of treatments
- $m \times n$  **structure matrix B** describes the structure of the network
  - rows correspond to the observed pairwise comparisons (studies)
  - columns represent treatments **pom**, **dex**, **pom+dex**

study 1:	<b>pom</b>	<i>vs</i>	<b>dex</b>
study 2:	<b>pom + dex</b>	<i>vs</i>	<b>dex</b>
study 3:	<b>pom + dex</b>	<i>vs</i>	<b>pom</b>
study 4:	<b>pom</b>	<i>vs</i>	<b>dex</b>

$$\mathbf{B} = \begin{pmatrix} 1 & -1 & 0 \\ 0 & -1 & 1 \\ -1 & 0 & 1 \\ 1 & -1 & 0 \end{pmatrix}$$

- **B** is the design matrix of the standard NMA model
- For sake of simplicity of presentation, we ignore that there may be multi-arm studies

# Additive CNMA model

- $n \times c$  **combination structure matrix C** describes how the  $n = 3$  treatments (here **pom**, **dex**, **pom + dex**) are composed of the  $c = 2$  components **pom** and **dex**

treatment 1:	<b>pom</b>	$\mathbf{C} = \begin{pmatrix} 1 & 0 \\ 0 & 1 \\ 1 & 1 \end{pmatrix}$
treatment 2:	<b>dex</b>	
treatment 3:	<b>pom + dex</b>	

- The **design matrix of the additive model** is the  $m \times c$  matrix **X**:

study 1:	<b>pom</b>	<i>vs</i>	<b>dex</b>	$\mathbf{X} = \mathbf{BC} = \begin{pmatrix} 1 & -1 \\ 1 & 0 \\ 0 & 1 \\ 1 & -1 \end{pmatrix}$
study 2:	<b>pom + dex</b>	<i>vs</i>	<b>dex</b>	
study 3:	<b>pom + dex</b>	<i>vs</i>	<b>pom</b>	
study 4:	<b>pom</b>	<i>vs</i>	<b>dex</b>	

# Interaction CNMA model

- $n \times c$  **combination structure matrix**  $\mathbf{C}^*$  describes how the  $n = 3$  treatments (here **pom**, **dex**, **pom + dex**) are composed of the  $c = 3$  components **pom**, **dex** and **pom+dex**:

treatment 1:	<b>pom</b>	$\mathbf{C}^* = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 1 & 1 & 1 \end{pmatrix}$
treatment 2:	<b>dex</b>	
treatment 3:	<b>pom+dex</b>	

- The **design matrix of the interaction model** is

study 1:	<b>pom</b>	<i>vs</i>	<b>dex</b>	$\mathbf{X} = \mathbf{B}\mathbf{C}^* = \begin{pmatrix} 1 & -1 & 0 \\ 1 & 0 & 1 \\ 0 & 1 & 1 \\ 1 & -1 & 0 \end{pmatrix}$
study 2:	<b>pom + dex + pom+dex</b>	<i>vs</i>	<b>dex</b>	
study 3:	<b>pom + dex + pom+dex</b>	<i>vs</i>	<b>pom</b>	
study 4:	<b>pom</b>	<i>vs</i>	<b>dex</b>	

# General CNMA model

The component NMA model (CNMA model) is

$$\mathbf{d} = \mathbf{X}\beta + \epsilon$$

where

- $\mathbf{d} \in \mathbb{R}^m$  is the vector of observed relative effects (differences) from the studies
- $\mathbf{X} = \mathbf{BC}$  is the design matrix (based on  $\mathbf{C}$  with an additive or  $\mathbf{C}^*$  with an interaction structure)
- $\beta \in \mathbb{R}^c$  is a parameter vector representing the components
- $\epsilon \in \mathbb{R}^m$  is a multivariate normally distributed error

Estimation via weighted least squares [Rücker et al., 2019b]

# Heterogeneity statistic for the CNMA model

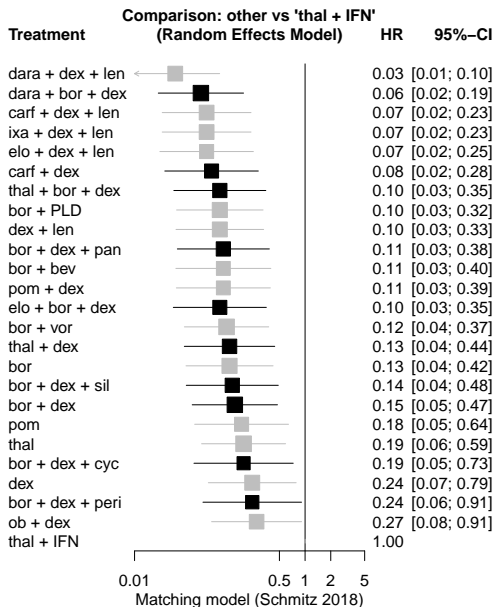
The heterogeneity statistic for the CNMA model is

$$Q = (\mathbf{d} - \hat{\delta})^T \mathbf{W}(\mathbf{d} - \hat{\delta})$$

where

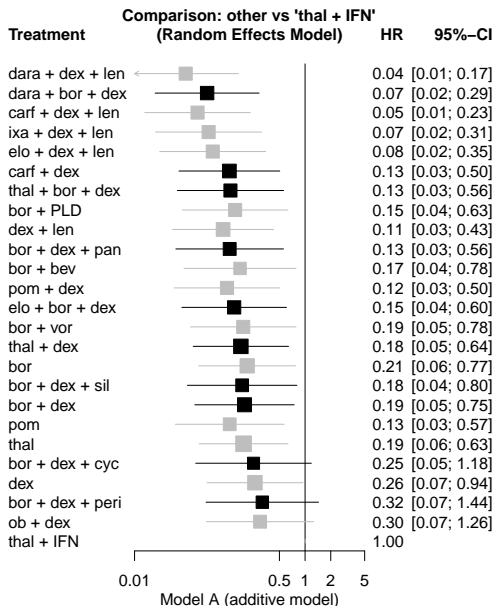
- $\hat{\delta}$  denotes the vector of estimates based on the CNMA model
- $\mathbf{W}$  is a  $m \times m$  weight matrix derived of inverse variances of the observed effects
- $Q$  approximately follows a  $\chi^2$  distribution with  $df = n_a - k - r$  degrees of freedom where
  - $n_a$  is the total number of arms in the network
  - $k$  is the total number of studies in the network
  - $r$  is the rank of the design matrix  $\mathbf{X}$

# Compare models: Matching method





# Compare models: Additive model



# Interaction CNMA models: Model selection

Starting from the additive model, add interaction terms in a systematic model selection procedure

Note:

- Only interactions corresponding to combinations observed in the data can be estimated
- Some interaction terms cannot be estimated (we'll come back to this in the discussion)

First idea: Find a sparse model that fits the data well!

# Interaction CNMA models: Model selection

## Sparse or not sparse?

- Usually, we want to avoid overfitting
- However, in a connected network, the standard NMA uses **all interactions** (all treatment combinations)!
- We cannot do this in a disconnected network
- But, why shouldn't we try to include in a disconnected network **as many interactions as possible**, before the network breaks up?

## Two possible procedures

- **Forward selection:** Starting from the (sparse) additive model, add interactions
- **Backward selection:** Starting from the (rich, but impossible) NMA model, separate single components

# Interaction CNMA models: Model selection

## Forward selection

- Start from the additive model (no interactions)
- Add (in turn) each two-way interaction that was observed in the data to the additive model
- Add (in turn) each three-way interaction that was observed in the data to the additive model
- Further candidate models by combining each two, three, ... interaction terms
- Select the final model based on comparing Cochran's Q statistic between nested models
- **Ideally, Q reduces to the sum of the Qs from the subnetworks**

# Interaction CNMA models: Model selection

- **Separate CNMA**
  - White network ( $Q = 0.30$ ,  $df = 2$ ,  $p = 0.8595$ )
  - Black network ( $Q = 0$ ,  $df = 0$ )
- **Additive model** ( $Q = 27.78$ ,  $df = 7$ ,  $p = 0.0002$ )
- **10 two-way interactions with data**
  - Three of them led to a reduction of the degrees of freedom and a reduction of  $Q$  ( $bor*dex$ ,  $pom*dex$ ,  $thal*dex$ )
  - Best:  **$bor*dex$**  ( $Q = 9.40$ ,  $df = 6$ ,  $p = 0.1523$ )
- **11 three-way interactions with data**
  - Only  **$carf*dex*len$**  considerably improved the model fit ( $Q = 9.47$ ,  $df = 6$ ,  $P = 0.1487$ )
- **Combining two (2-way or 3-way) interaction terms**
  - Best:  **$bor*dex + carf*dex*len$**  ( $Q = 0.91$ ,  $df = 5$ ,  $p = 0.9699$ )

# Interaction CNMA models: Model selection

Best models with more than two interaction terms

- **Combining three interaction terms**

- $\text{bor}^*\text{dex} + \text{carf}^*\text{dex}^*\text{len} + \text{thal}^*\text{bor}^*\text{dex}$   
( $Q = 0.86$ ,  $df = 4$ ,  $p = 0.9301$ )

- **Combining four interaction terms**

- $\text{bor}^*\text{dex} + \text{carf}^*\text{dex}^*\text{len} + \text{thal}^*\text{bor}^*\text{dex} + \text{dara}^*\text{bor}^*\text{dex}$   
( $Q = 0.33$ ,  $df = 3$ ,  $p = 0.9553$ )

- **Combining five interaction terms**

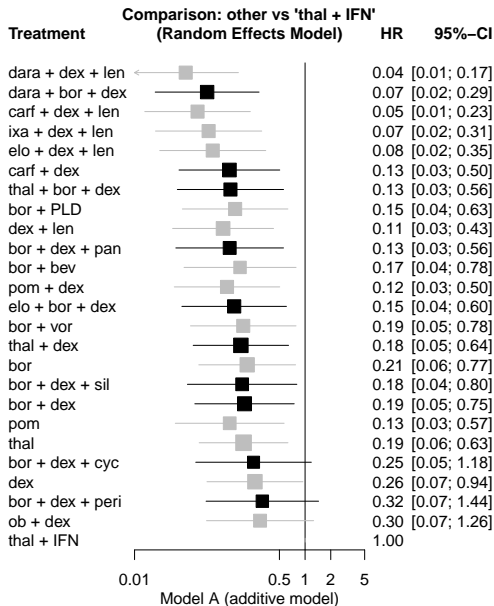
- $\text{bor}^*\text{dex} + \text{carf}^*\text{dex}^*\text{len} + \text{thal}^*\text{bor}^*\text{dex} + \text{dara}^*\text{bor}^*\text{dex} + \text{elo}^*\text{bor}^*\text{dex}$   
( $Q = 0.30$ ,  $df = 2$ ,  $p = 0.8595$ )
- This is a saturated model as it achieves the fit of the white network  
( $Q = 0.30$ ,  $df = 2$ ,  $p = 0.8595$ )  $\Rightarrow$  No further improvement possible
- The saturated model is not significantly better than the sparser model  $\text{bor}^*\text{dex} + \text{carf}^*\text{dex}^*\text{len}$   
( $Q$  test for difference:  $Q_{\text{diff}} = 0.60$ ,  $df = 3$ ,  $p = 0.8959$ )

# Interaction CNMA models: Model selection

## Backward selection

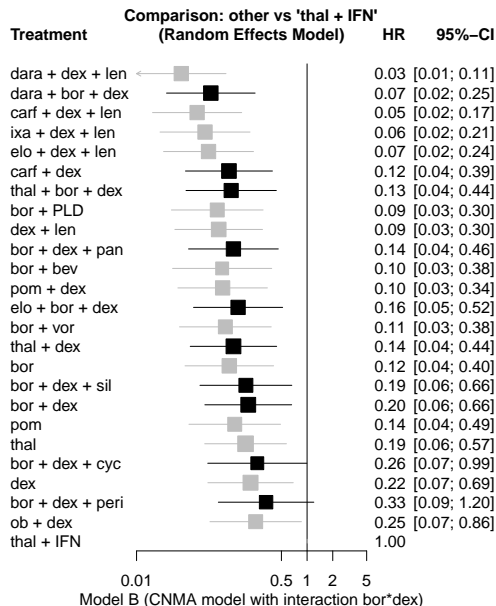
- Start with isolating only **one** component, for example **thal**
- Technically, define a matrix  $C^{**}$  with all combinations and replace column **thal** with a column with ones for all treatment combinations that contain **thal** as a component
- **thal** is in the white network, but **thal + dex** is in the black network  
⇒ sufficient to connect the subnetworks
- Surprisingly, this (rich) model corresponds to another saturated model, but with slightly different estimates ( $Q = 0.30$ ,  $df = 2$ ,  $p = 0.8595$ )
- Same works with **bor**, **carf**, **dara**, or **elo**

# Additive model (Q = 27.78, df = 7, p = 0.0002)

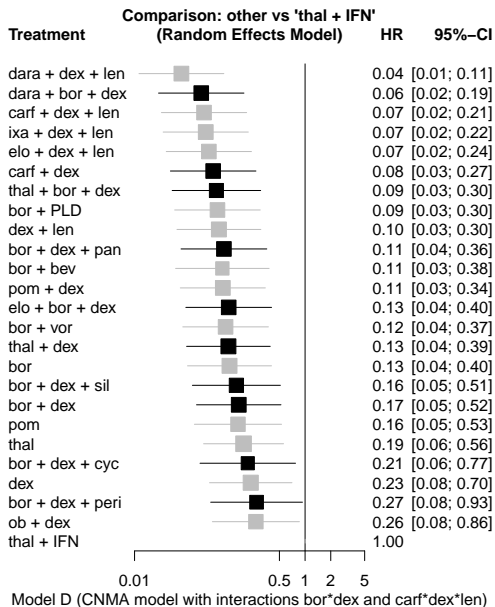




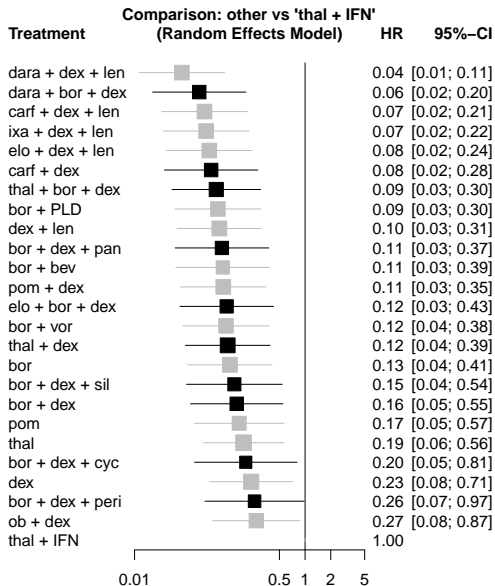
# Model with bor\*dex (Q = 9.40, df = 6, p = 0.152)



bor\*dex + carf\*dex\*len (Q = 0.91, df = 5, p = 0.970)

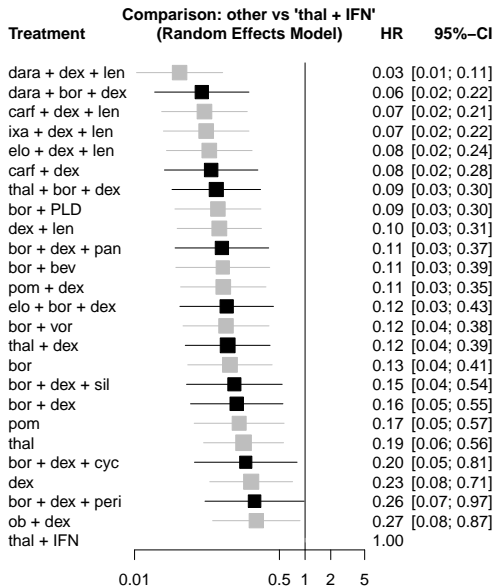


# Three interactions (Q = 0.86, df = 4, p = 0.930)



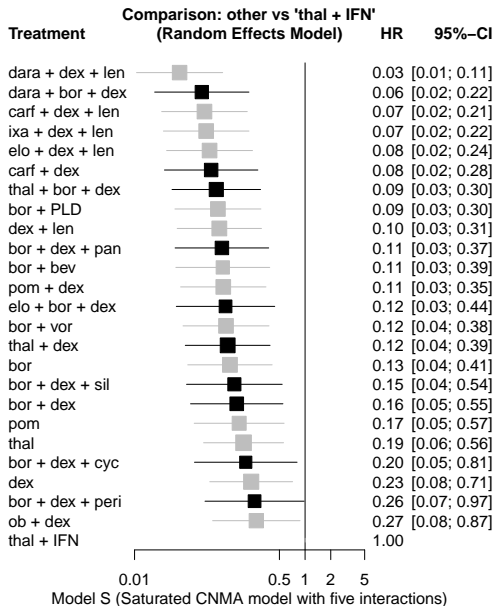
Model E (CNMA model with interactions bor\*dex, carf\*dex\*len and thal\*bor\*dex)

# Four interactions (Q = 0.33, df = 3, p = 0.955)

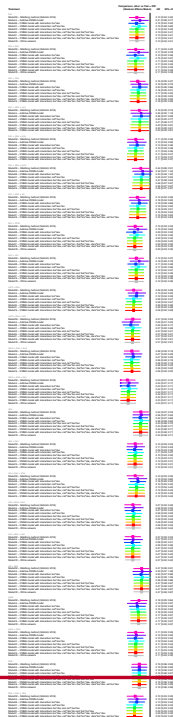


Model F (CNMA model with interactions bor\*dex + carf\*dex\*len + thal\*bor\*dex + dara\*bor\*dex)

# Saturated model ( $Q = 0.30$ , $df = 2$ , $p = 0.860$ )



# Compare all models: Forest plot



carf + dex

- Model M – Matching method (Schmitz 2018)
- Model A – Additive CNMA model
- Model B – CNMA model with interaction bor\*dex
- Model C – CNMA model with interaction carf\*dex\*len
- Model D – CNMA model with interactions bor\*dex and carf\*dex\*len
- Model E – CNMA model with interactions bor\*dex, carf\*dex\*len and thal\*bor\*dex
- Model F – CNMA model with interactions bor\*dex, carf\*dex\*len, thal\*bor\*dex, dara\*bor\*dex
- Model S – CNMA model with interactions bor\*dex, carf\*dex\*len, thal\*bor\*dex, dara\*bor\*dex, elo\*bor\*dex



0.08	[0.02; 0.28]
0.13	[0.03; 0.50]
0.12	[0.04; 0.39]
0.08	[0.02; 0.27]
0.08	[0.03; 0.27]
0.08	[0.02; 0.28]
0.08	[0.02; 0.28]
0.08	[0.02; 0.28]

carf + dex + len

- Model M – Matching method (Schmitz 2018)
- Model A – Additive CNMA model
- Model B – CNMA model with interaction bor\*dex
- Model C – CNMA model with interaction carf\*dex\*len
- Model D – CNMA model with interactions bor\*dex and carf\*dex\*len
- Model E – CNMA model with interactions bor\*dex, carf\*dex\*len and thal\*bor\*dex
- Model F – CNMA model with interactions bor\*dex, carf\*dex\*len, thal\*bor\*dex, dara\*bor\*dex
- Model S – CNMA model with interactions bor\*dex, carf\*dex\*len, thal\*bor\*dex, dara\*bor\*dex, elo\*bor\*dex
- Model W – White network



0.07	[0.02; 0.23]
0.05	[0.01; 0.23]
0.05	[0.02; 0.17]
0.07	[0.02; 0.26]
0.07	[0.02; 0.21]
0.07	[0.02; 0.21]
0.07	[0.02; 0.21]
0.07	[0.02; 0.21]
0.07	[0.02; 0.21]

dara + bor + dex

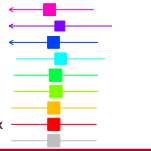
- Model M – Matching method (Schmitz 2018)
- Model A – Additive CNMA model
- Model B – CNMA model with interaction bor\*dex
- Model C – CNMA model with interaction carf\*dex\*len
- Model D – CNMA model with interactions bor\*dex and carf\*dex\*len
- Model E – CNMA model with interactions bor\*dex, carf\*dex\*len and thal\*bor\*dex
- Model F – CNMA model with interactions bor\*dex, carf\*dex\*len, thal\*bor\*dex, dara\*bor\*dex
- Model S – CNMA model with interactions bor\*dex, carf\*dex\*len, thal\*bor\*dex, dara\*bor\*dex, elo\*bor\*dex



0.06	[0.02; 0.19]
0.07	[0.02; 0.29]
0.07	[0.02; 0.25]
0.06	[0.02; 0.19]
0.06	[0.02; 0.19]
0.06	[0.02; 0.20]
0.06	[0.02; 0.22]
0.06	[0.02; 0.22]

dara + dex + len

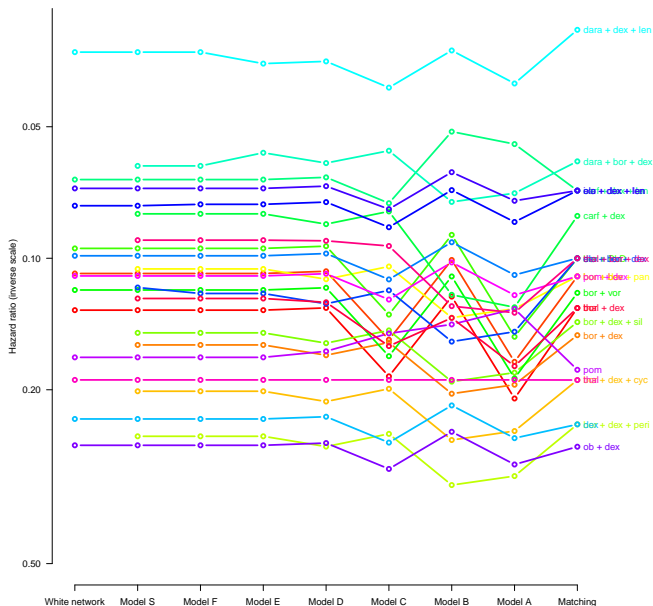
- Model M – Matching method (Schmitz 2018)
- Model A – Additive CNMA model
- Model B – CNMA model with interaction bor\*dex
- Model C – CNMA model with interaction carf\*dex\*len
- Model D – CNMA model with interactions bor\*dex and carf\*dex\*len
- Model E – CNMA model with interactions bor\*dex, carf\*dex\*len and thal\*bor\*dex
- Model F – CNMA model with interactions bor\*dex, carf\*dex\*len, thal\*bor\*dex, dara\*bor\*dex
- Model S – CNMA model with interactions bor\*dex, carf\*dex\*len, thal\*bor\*dex, dara\*bor\*dex, elo\*bor\*dex
- Model W – White network



0.03	[0.01; 0.10]
0.04	[0.01; 0.17]
0.03	[0.01; 0.11]
0.04	[0.01; 0.14]
0.04	[0.01; 0.11]
0.04	[0.01; 0.11]
0.03	[0.01; 0.11]
0.03	[0.01; 0.11]

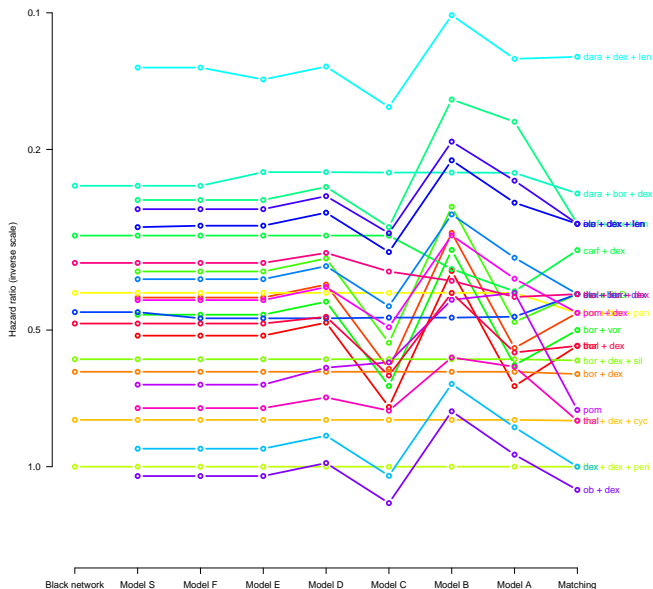


# Compare all models to the white network: Line plot



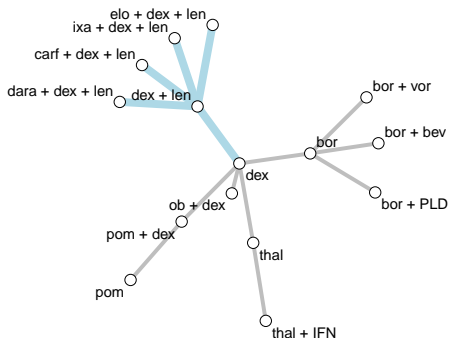


# Compare all models to the black network: Line plot



# Possible overparameterization in CNMA models

- In a CNMA model only observed interactions can be tested
- Some observed interactions can be formally included, but do not add to the model because they are not estimable
  - Example dex + len:  
Either compared to  $X + \text{dex} + \text{len}$  (estimates  $X$ ) or to dex alone (such that  $\text{dex} * \text{len}$  cannot be separated from len alone)



# Discussion I

- All models rely on assumptions
  - **Matching method** assumes no unmeasured confounders
  - **CNMA** assumes no unmeasured interactions
    - **Forward selection - from sparse to rich:** stepwise mitigate the additivity assumptions
    - **Backward selection - from rich to sparse:** isolate only a single component (or a small number of components) and thus avoid assumptions of additivity as far as possible
  - **All models** make the usual assumptions of NMA, such as transitivity of effect moderators across different studies
- Limitation of matching method
  - Relies on external evidence from observational studies
  - Time-consuming

# Discussion II

- Aims of CNMA
  - To fit the model to the given data
- This case study
  - allowed to fit an overarching model to both networks
    - while perfectly reproducing (via interactions) the analyses of the separate networks
  - compared the results to those of the matching method
    - not necessarily to reproduce them, but
    - finding wide agreement with the matching method results
- Ideally, clinical knowledge should be incorporated to inform the model and critically assess the results

# Summary

- CNMA models allow
  - **estimating effects** of treatment components of multicomponent interventions
  - **comparing estimates** and model fit to the standard NMA using likelihood ratio statistics
  - **borrowing strength** from studies with common components
  - **bridging the gap** between disconnected networks
- Implemented in R package **netmeta** [Rücker et al., 2019a]
  - `netcomb()` for connected networks
  - `discomb()` for disconnected networks
- Similar (Bayesian) approaches [Welton et al., 2009, Mills et al., 2012]
  - Applications [Caldwell and Welton, 2016, Freeman et al., 2017, Pompoli et al., 2018]

# References I



Caldwell, D. M. and Welton, N. J. (2016).

Approaches for synthesising complex mental health interventions in meta-analysis.

*Evidence-Based Mental Health*, 19(1):16–21.



Freeman, S. C., Scott, N. W., Powell, R., Johnston, M., Sutton, A. J., and Cooper, N. J. (2017).

Component network meta-analysis identifies the most effective components of psychological preparation for adults undergoing surgery under general anesthesia.

*Journal of Clinical Epidemiology*.

doi: 10.1016/j.jclinepi.2018.02.012.



Mills, E. J., Thorlund, K., and Ioannidis, J. P. (2012).

Calculating additive treatment effects from multiple randomized trials provides useful estimates of combination therapies.

*Journal of Clinical Epidemiology*, 65(12):1282–1288.

doi: 10.1016/j.jclinepi.2012.07.012.



Pompoli, A., Furukawa, T. A., Efthimiou, O., Imai, H., Tajika, A., and Salanti, G. (2018).

Dismantling cognitive-behaviour therapy for panic disorder: a systematic review and component network meta-analysis.

*Psychological Medicine*, pages 1–9.

doi:10.1017/S0033291717003919.



R Core Team (2019).

*R: A Language and Environment for Statistical Computing*.

R Foundation for Statistical Computing, Vienna, Austria.



Rücker, G., Krahn, U., König, J., Efthimiou, O., and Schwarzer, G. (2019a).

netmeta: Network meta-analysis using frequentist methods.

R package version 1.1-0.



Rücker, G., Petropoulou, M., and Schwarzer, G. (2019b).

Network meta-analysis of multicomponent interventions.

*Biometrical Journal*.

# References II



Schmitz, S., Maguire, Á., Morris, J., Ruggeri, K., Haller, E., Kuhn, I., Leahy, J., Homer, N., Khan, A., Bowden, J., Buchanan, V., O'Dwyer, M., Cook, G., and Walsh, C. (2018).  
The use of single armed observational data to closing the gap in otherwise disconnected evidence networks: a network meta-analysis in multiple myeloma.  
*BMC Medical Research Methodology*, 18(1):66.



Sturtz, S., Ligges, U., and Gelman, A. (2005).  
R2WinBUGS: A package for running WinBUGS from R.  
*Journal of Statistical Software*, 12(3):1–16.



Welton, N. J., Caldwell, D. M., Adamopoulos, E., and Vedhara, K. (2009).  
Mixed treatment comparison meta-analysis of complex interventions: psychological interventions in coronary heart disease.  
*American Journal of Epidemiology*, 169(9):1158–1165.  
doi: 10.1093/aje/kwp014.

# Connecting networks by isolating a component (thal)

