



EFSPI & BBS “Small populations and level of evidence”

Bayesian analysis for small sample size trials using informative priors derived from historical data



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Introduction

Planning a trial in patients with $\Delta F508$ mutation in cystic fibrosis at early clinical development

- // Cystic fibrosis is a multi-organ disorder
 - // Caused by gen mutations, cystic fibrosis transmembrane conductance regulator (CFTR) channels are affected; most frequent mutation is $\Delta F508$
 - // Today survival depends on status of lung disease, median age of survival is 40 years
 - // Rare disease: Affects ≈ 1 out of 3000 newborns of Northern European ancestry, ≈ 30000 patients with CF in USA
- // At early clinical development, trials are conducted to evaluate the treatment potential of drug
 - // Desire to conduct trials with small sample sizes
 - // Large challenges in recruiting patients for trials in rare disease like cystic fibrosis
 - // Limit number of patients to be exposed to drug without proven clinical benefit
 - // Fast decision making to avoid delaying development of potential efficacious drug
 - // Utilize historical information by using Bayesian approach
 - // Replace real patients by “virtual” patients \rightarrow reduce sample size



Trial design and historical data

Early clinical development trial in patients with $\Delta F508$ mutation in cystic fibrosis

- // Randomized, placebo-controlled, parallel group trial in cystic fibrosis patients with by $\Delta F508$ mutation
- // Primary variable: Change of sweat chloride (Cl) content from baseline
 - // Sweat Cl content is established diagnostic and biomarker for clinical trials for cystic fibrosis
- // Primary objective: Evaluate reduction of sweat Cl content from baseline under treatment vs. placebo
- // Approach: Use historical data to reduce number of patient with $\Delta F508$ mutation for placebo treatment
 - // Historical data for change from baseline of sweat Cl content (mmol/L) in patients treated with placebo

Source	Gender	Age	FEV1 pred.	Genotype	Time	N	Mean	St. dev.
Clancy et.al., Thorax (2012)	F & M	18 - 54	$\geq 40\%$	F508del-CFTR, homozygote	Day 14	17	1.75	7.7
Flume et.al., Chest (2012)	F & M	12 - 52	$\geq 40\%$	F508del-CFTR, homozygote	Day 15	26	-0.04	8.1
Boyle et.al., Lancet (2014)	F & M	≥ 18	$\geq 40\%$	F508del-CFTR, homozygote	Day 14	21	-1.7	8.7
Ramsey et.al., N Engl J Med (2011)	F & M	12 - 53	31.6 - 98.2	G551D-CFTR, homozygote	Day 15	74	-0.15	7.8

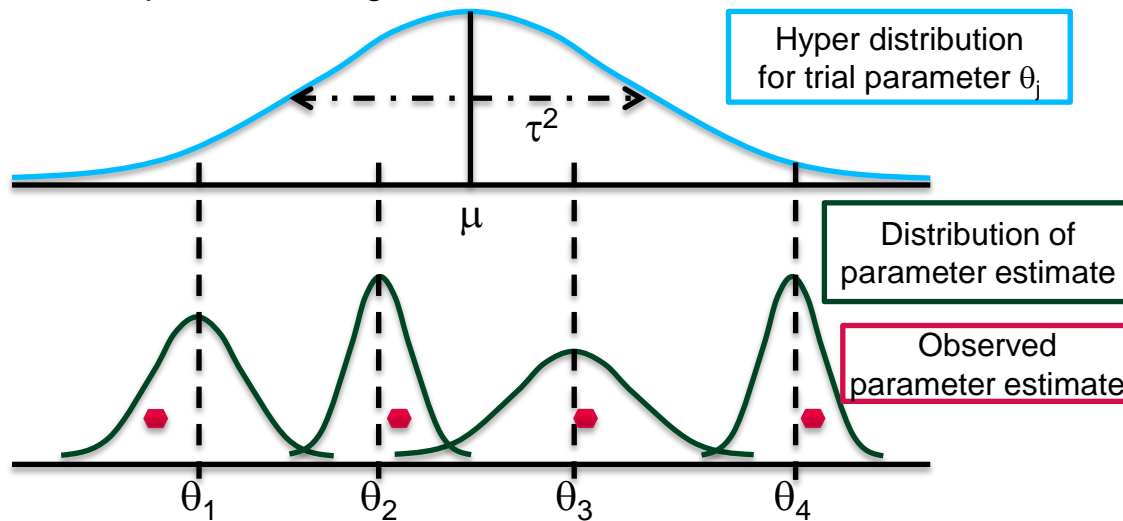
- // Selection of data based on external expert feedback (status of 2015)
 - // Similar changes for both genotypes for placebo
 - // Inclusion of recent articles to ensure comparable measurement procedure for sweat Cl
- // Between trial-variability for mean and potentially for standard deviation

Deriving prior distribution from historical data sources

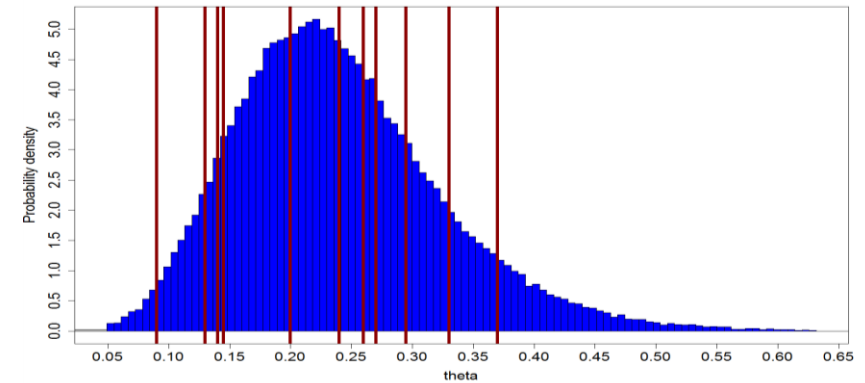
Using meta-analytical prediction to deal with between-trial variability

- // Deriving prior distribution for placebo by simple pooling of historical data ignores between-trial variability
- // Would lead to overestimation of existing information
- // Meta-analytical prediction (MAP) approach allows deriving of prior distribution while taking uncertainty due to between-trial variability into account [Neuenschwander et al. (2010), Schmidli et al. (2014)]

1. Bayesian random-effect meta analysis on historical data for trial parameter, e.g. means



2. Predicted posterior distribution for parameter θ^* in new trial



Predicted posterior distribution
 = Hyper distribution + uncertainty in estimates of μ and τ^2

- // Predicted posterior distribution for parameter θ^* in new trial reflects all information about this parameter

Modelling estimates for mean and variance for placebo in trials

MAP: Model for Bayesian random-effect meta analysis for sweat CI content

// Response y_{ij} , $i = 1, \dots, n_j$ of patient i in trial j is normal distributed with unknown, trial-specific mean ϑ_j and variance σ_j^2

$$y_{ij} | \vartheta_j, \sigma_j^2 \sim N(\vartheta_j, \sigma_j^2)$$

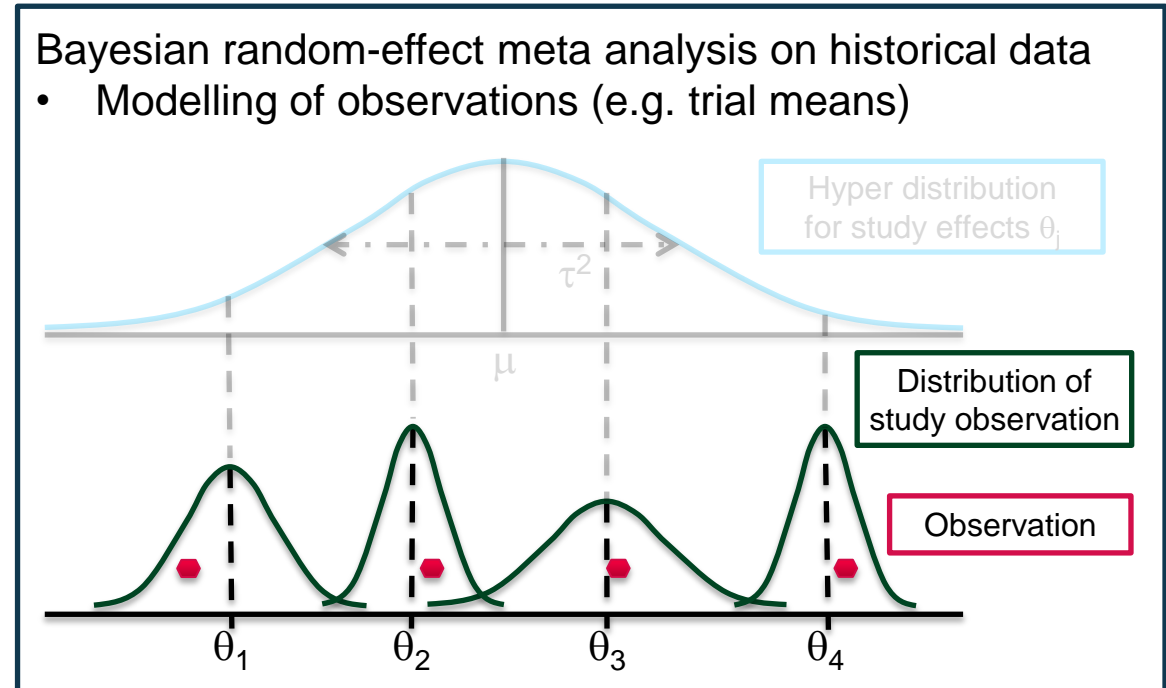
// Observed mean response M_j of trial j follows a normal distribution

$$M_j | \vartheta_j, \sigma_j^2 \sim N\left(\vartheta_j, \frac{\sigma_j^2}{n_j}\right)$$

// Observed variance of response S_j^2 of trial j follows a “scaled” χ^2 -distribution

$$S_j^2 | \sigma_j^2 \sim \chi^2(n_j - 1, \sigma_j^2)$$

i.e. $S_j^2 / \sigma_j^2 \sim \chi^2(n_j - 1)$ follows a χ^2 -distribution with $n_j - 1$ degree of freedom



Modelling the unknown means of sweat Cl content in trials

MAP: Model for Bayesian random-effect meta analysis for sweat Cl content

// For modelling the means ϑ_j of the trials, a normal distribution is used with unknown mean μ and variance τ^2 as hyper distribution

$$\vartheta_j | \mu, \tau^2 \sim N(\mu, \tau^2)$$

// Weak informative prior distributions for hyper distribution parameters are used

// Mean $\mu \sim$ Normal distribution

// mean = 0, variance = 5^2

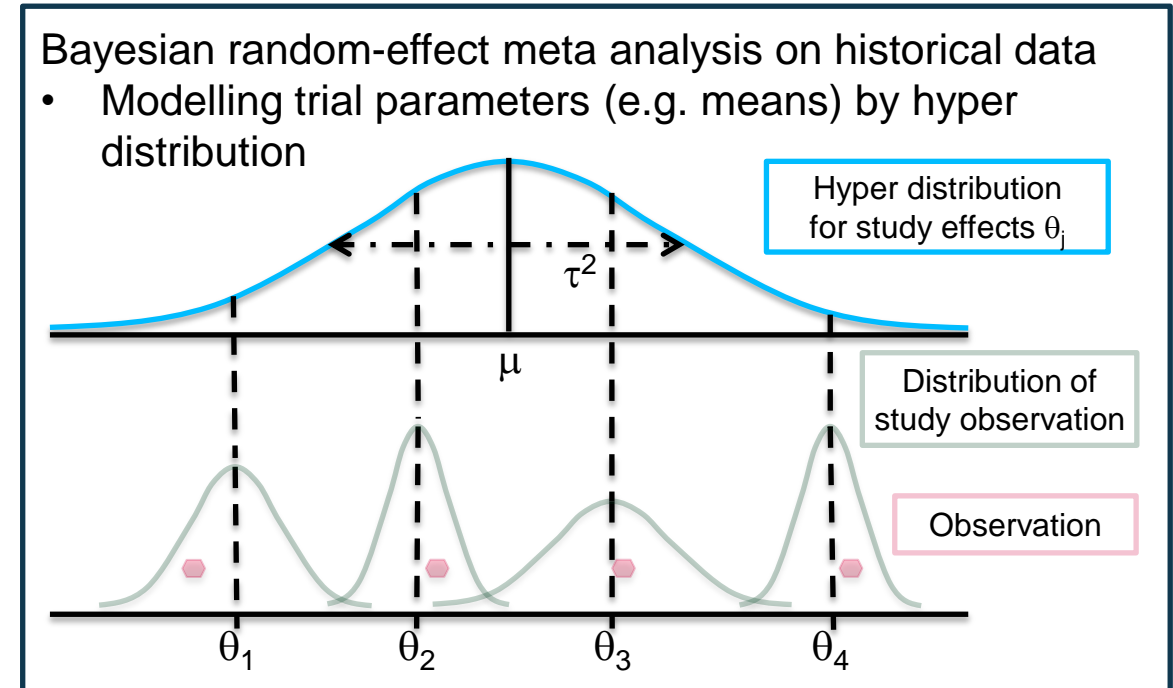
// Variance $\tau^2 \sim$ Gamma distribution

// mean = 1.5^2 , CV = 100%

// Use of informative priors to cope with small numbers of historical trials [Wandel et al. (2017), Friede et al. (2017)]

// Values were chosen to restrict μ and τ^2 on plausible values while avoiding “over domination”

// Evaluation of impact of informative priors in meta-analysis by sensitivity analysis





Modelling the unknown variance of sweat Cl content in trials

MAP: Model for Bayesian random-effect meta analysis for sweat Cl content

- // For modelling the variance σ_j^2 of the trials, an inverse-gamma distribution is used as hyper distribution
 - // To allow easier assessing of between-trial variability of variance, the inverse gamma distribution is reparametrized by the mean δ^2 and the coefficient of variation ε

$$\sigma_j^2 | \delta^2, \varepsilon \sim \text{Inv} - \Gamma(2 + 1/\varepsilon^2, \delta^2 (1 + 1/\varepsilon^2))$$

- // Weak informative prior distributions for hyper distribution parameters are used
 - // Mean $\delta^2 \sim$ Gamma distribution
 - // mean = 8^2 , CV = 100%
 - // Coefficient of variation $\varepsilon \sim$ Gamma distribution
 - // mean = 20%, CV = 100%
- // Remark: For common variance, $\sigma^2 = \sigma_j^2$, replace hyper-distribution by inverse-gamma distribution for σ^2 as prior distribution
 - // Affects mainly variance estimates of studies, small impact on marginal posterior for trial means

Results of Bayesian meta-analysis for sweat Cl content for placebo

Results of first step of meta-analytical prediction

- // Posterior distribution for parameter of hyper-distributions are derived by MCMC simulations
- // Assessment of posterior probabilities provide insight about “reproducibility” of endpoints

// Trial means ϑ_j

// Located around $\mu \approx 0$

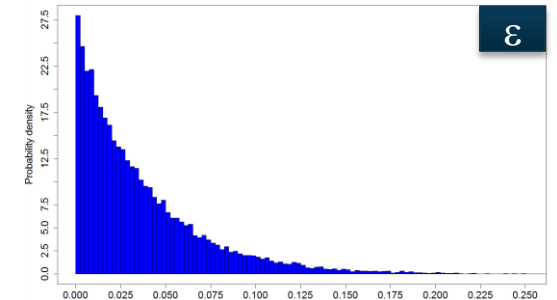
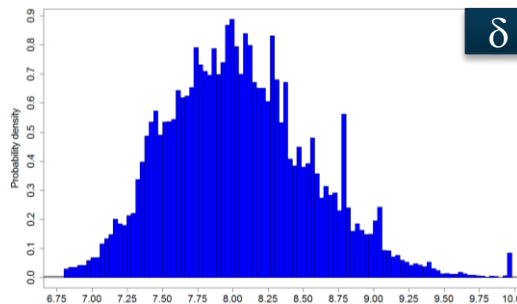
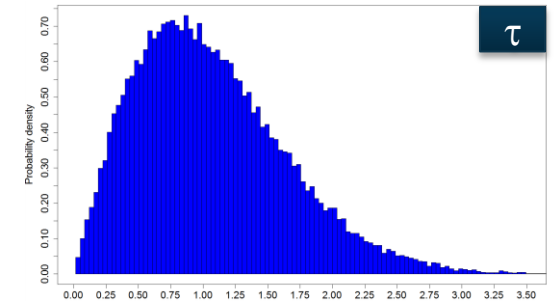
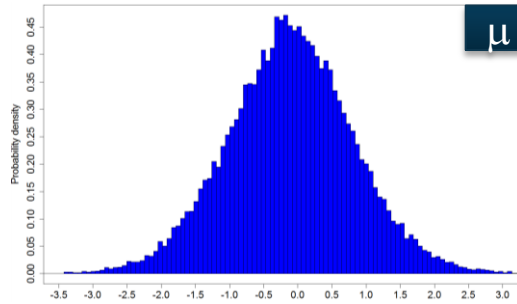
// Small between-trial variability, $\tau \approx 1$

// Variance of trials σ_j^2

// Located around $\delta^2 \approx 8^2$

// Negligible between-trial variability, $\varepsilon \approx 4\%$

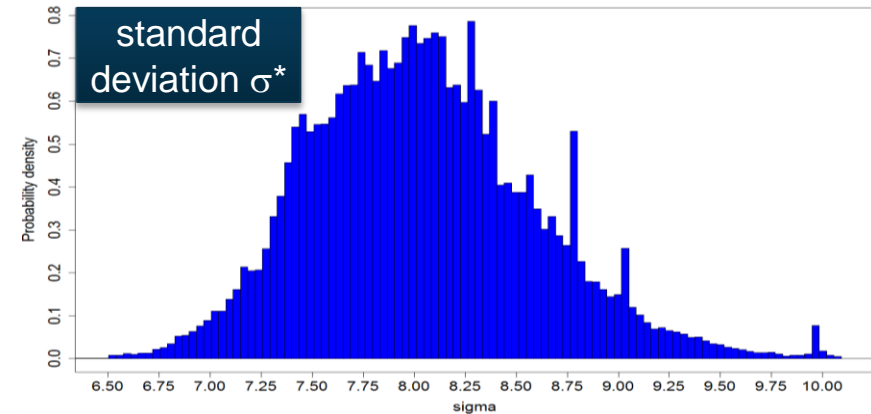
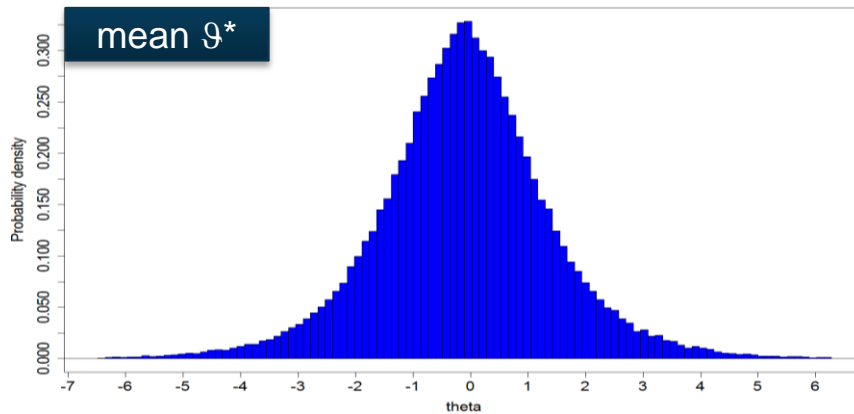
// Remark: Peaks in histogram for δ indicate convergence issues in MCMC simulation caused by limited information from data due to few studies → need for informative priors



Information about mean and variance of future trials

Results of prediction step of meta-analytical prediction

- // Knowledge about mean ϑ^* and variance σ^{*2} of a future trial is reflected by the hyper distributions taking uncertainties in for distribution parameters into account
- // Predicted posterior distribution for ϑ^* and σ^{*2} is a representation for the available information
- // MC samples for ϑ^* and σ^{*2} are derived from hyper distribution using MCMC parameter samples
- // Marginal predicted posterior distribution for trial mean ϑ^* and standard deviation σ^*



Parameter	mean	sd	q1	median	q3	90%-range_low	90%-range_up
Mean of new trial ϑ^*	-0.11	1.54	-0.98	-0.11	0.76	-2.58	2.37
Standard deviation of new trial σ^*	8.04	0.56	7.65	8.01	8.38	7.21	9.02



Deriving prior distribution for sweat Cl content for Bayesian analysis

Use predicted posterior distribution for future trial from MAP to derive prior information

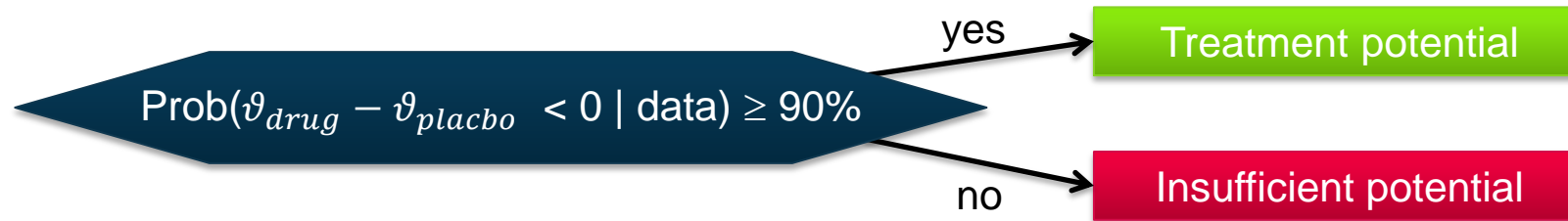
- // The predicted posterior distribution for ϑ^* and σ^{*2} reflects all prior information for mean and variance
 - // Use predicted posterior distribution as prior distribution for placebo
- // Derive analytical form for prior distribution by fitting a Normal – Inv- χ^2 distribution to MC samples of predicted posterior distribution

$$\vartheta_{placebo}, \sigma_{placebo}^2 \sim \text{Normal} - \text{Inv-}\chi^2(\text{mean} = -0.1, \text{kappa} = 27.8, \text{dof} = 106.3, \text{sd}^2 = 8^2)$$

- // Trial mean for placebo: Amount of information corresponds to ≈ 28 patients (kappa = 27.8)
 - // $\cong 20\%$ of total sample size in historical trials (N=138)
 - information reduction caused by between-trial variability
- // Trial variance for placebo: Amount of information corresponds to ≈ 107 patients (dof = 106.3)
 - // $\cong 80\%$ of total sample size
 - small information reduction due to negligible between-trial variability
- // Remark: To cope with long tails and/or shape deviations from standard distribution, deflate prior distribution (information loss) or use approximation by mixture distribution [Schmidli et al. (2014)]

Evaluation of treatment potential of drug using Bayesian approach

// Assessment of treatment potential by Bayesian analysis: Evaluate difference in mean change of sweat CI content from baseline between drug and placebo $\vartheta_{drug} - \vartheta_{placbo}$



// Marginal posterior probability for mean change of sweat CI from baseline for placebo ϑ_{placbo}

// Incorporate prior information for placebo derived by MAP procedure

// Based on expert feedback, no further deflation of prior despite potential domination over data

// Marginal posterior probability for mean change of sweat CI from baseline for drug ϑ_{drug}

// Vague prior information

// Posterior distribution for mean difference $\vartheta_{drug} - \vartheta_{placbo}$

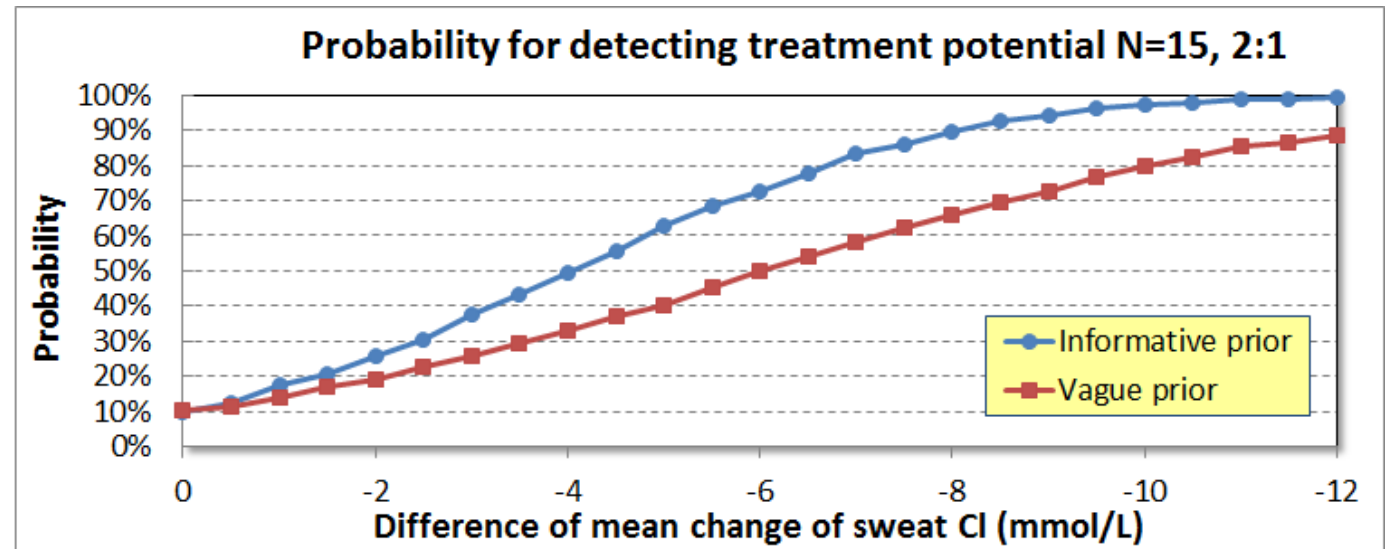
// MC sampling from marginal posterior distributions for ϑ_{placbo} and ϑ_{drug}

// Take differences of MC samples for drug and placebo

Operational characteristic of assessment of treatment potential

- // Capability of planned trial to detect treatment potential is evaluated by trial simulations
 - // Assess probability for detecting treatment potential for fixed difference in means $\vartheta_{drug} - \vartheta_{placbo}$
 - // Coping with uncertainty about ϑ_{placbo} and σ_{placbo}^2 : Sample parameters and averaging probability using prior distribution derived by MAP [Walley et.al. (2015)]; for drug higher variability is assumed $\sigma_{drug} = 1.1 \cdot \sigma_{placbo}$

- // Sample size determination
 - // 2:1 randomization
 - // $n_{drug} = 10$ and $n_{placbo} = 5$
 - // $\vartheta_{drug} - \vartheta_{placbo} = -8$ mmol/L
→ ≈ 90% probability for detecting treatment potential on average



- // Incorporation of prior information increases probability to detect treatment potential
 - // Allows designing trial with smaller sample sizes and unbalanced randomization



Summary and conclusions

- // Trials with small sample sizes are desired in rare disease, in particular at early stage of development
- // Incorporation of historical information might allow reduction of patient numbers
 - // Bayesian approach provides formal framework for incorporation of prior information in trial analysis
 - // Relevant sample size reduction can be achieved for small trials allowing imbalanced designs
- // Selection of historical data is a crucial step when deriving prior information for Bayesian analysis
 - // Close interaction with clinicians and experts is essential
 - // Meta-analytical prediction is a useful approach to derive prior distributions from historical source
 - // Cope with between-trial variability, thus prevents overestimation of information
 - // Usually effective sample size of derived prior distribution is much smaller than total sample size
 - // Provides additional insight about e.g. mean and variance of treatment response
 - // Meta-analysis on few historical trials is feasible when incorporating (weak) informative priors
 - // Evaluate impact of incorporating informative prior by sensitivity analysis
- // Domination of prior information in analysis and deflation of prior distribution needs to be considered



Thank you!



Bye-Bye

